



Data analysis for observing the Universe with Gravitational Waves at low frequency

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Workshop "Artificial Intelligence for HPC@Exscale"

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irfu

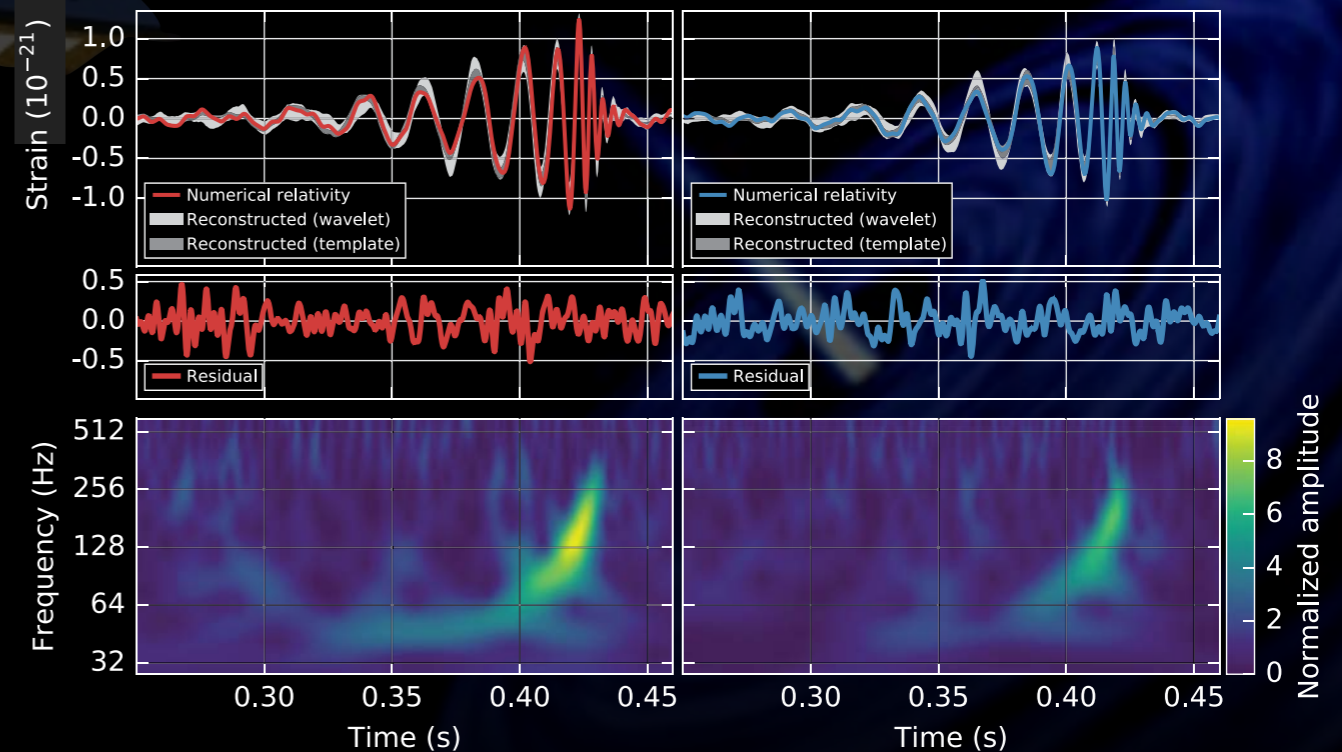
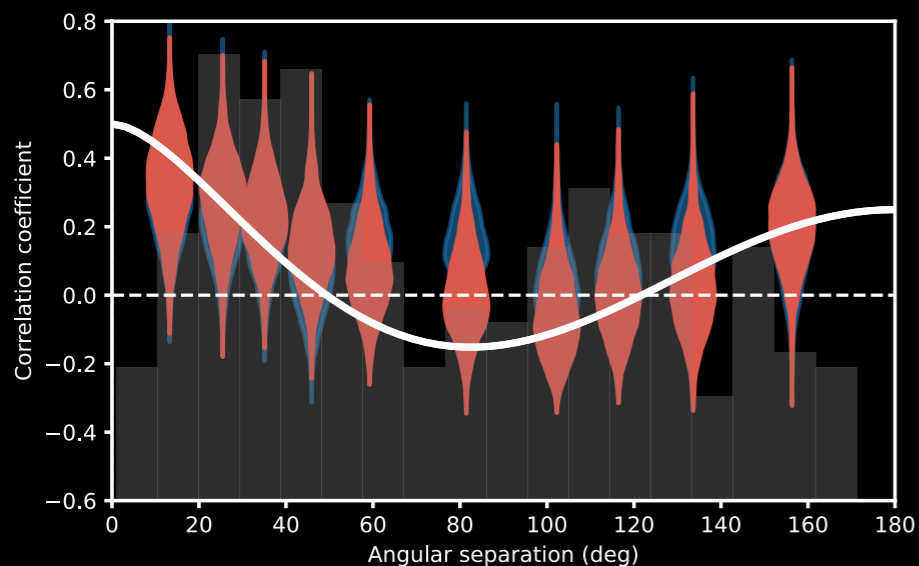
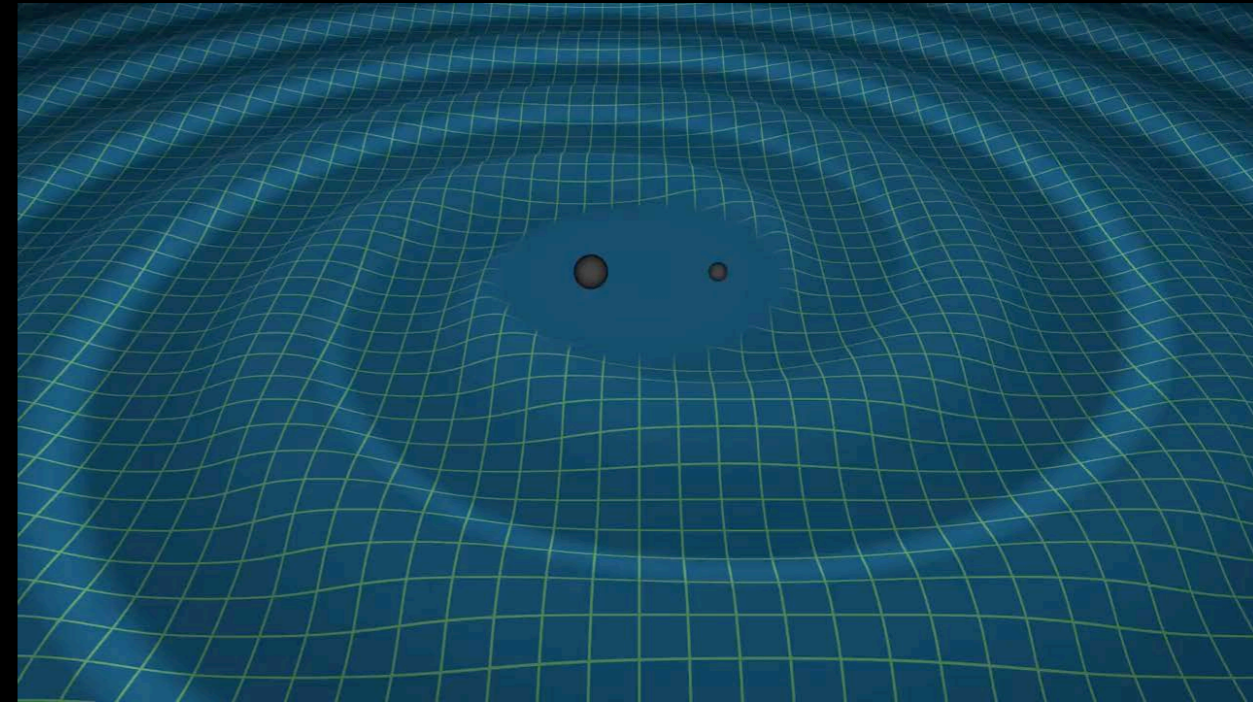


Observatoire de Paris

Gravitational waves (GWs)



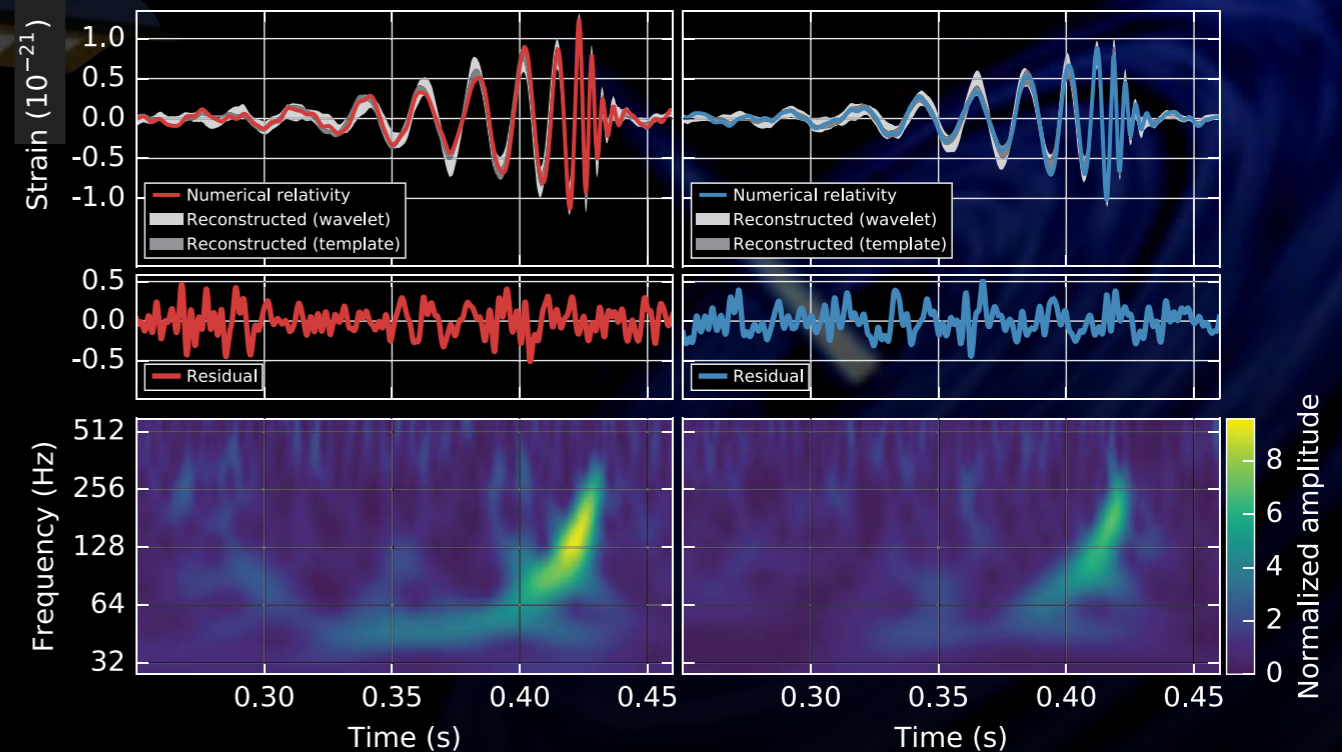
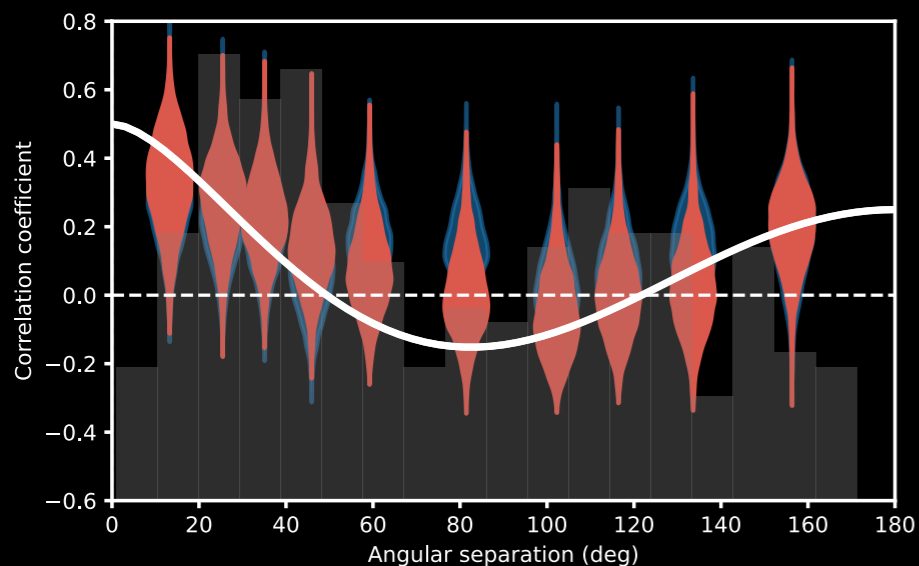
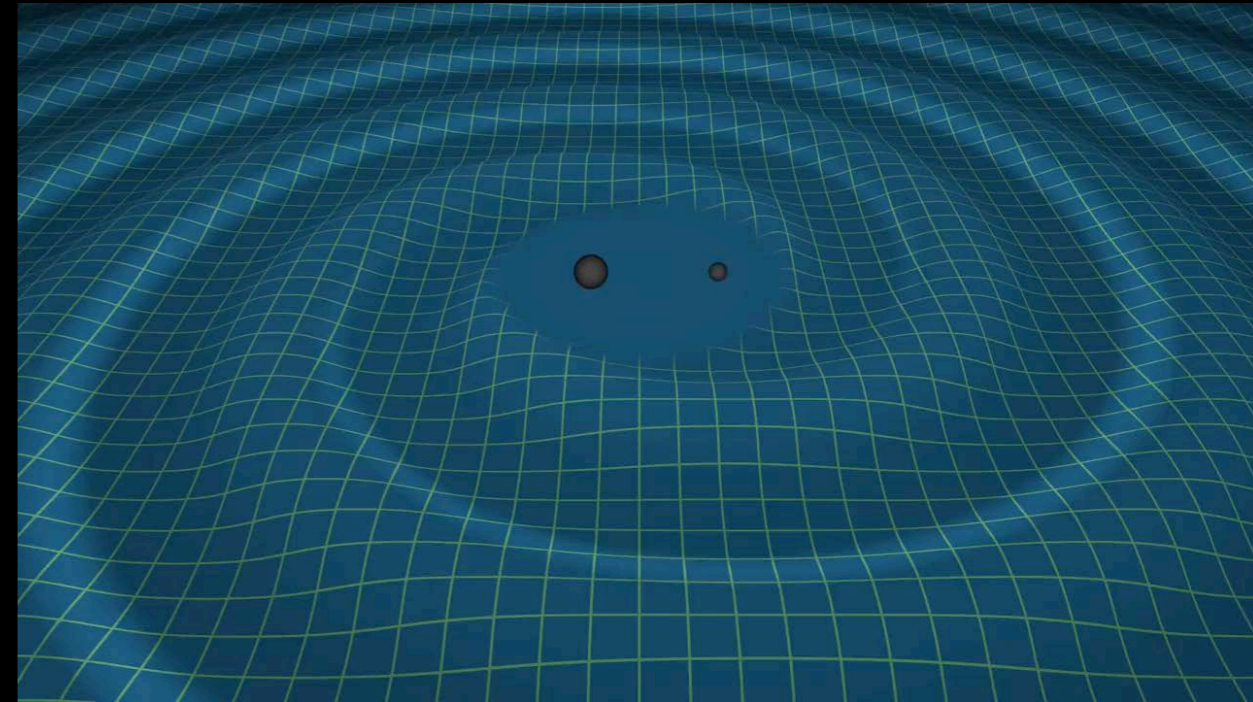
- ▶ General Relativity:
 - Space is deformed by its mass content;
 - Energy dissipation in the deformation of space-time => **Gravitational Waves (GWs)**
- ▶ Created when there is non-spherical acceleration of one or several bodies => typical source : binary
- ▶ New way to **observe the Universe**
- ▶ **GWs are real!**
 - Already detected at high frequency (LIGO/Virgo)
 - Strong evidence at very low frequency (PTA)



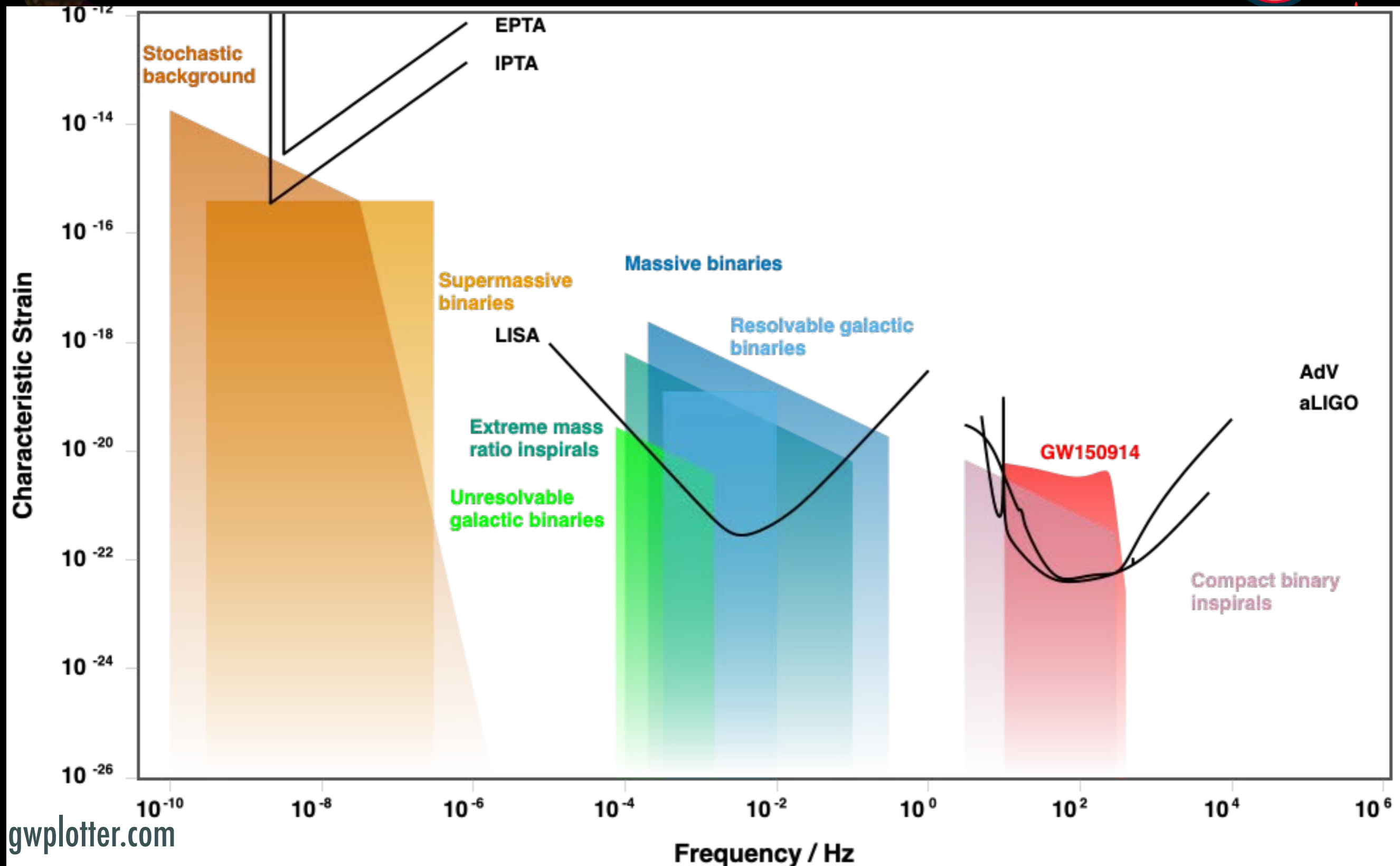
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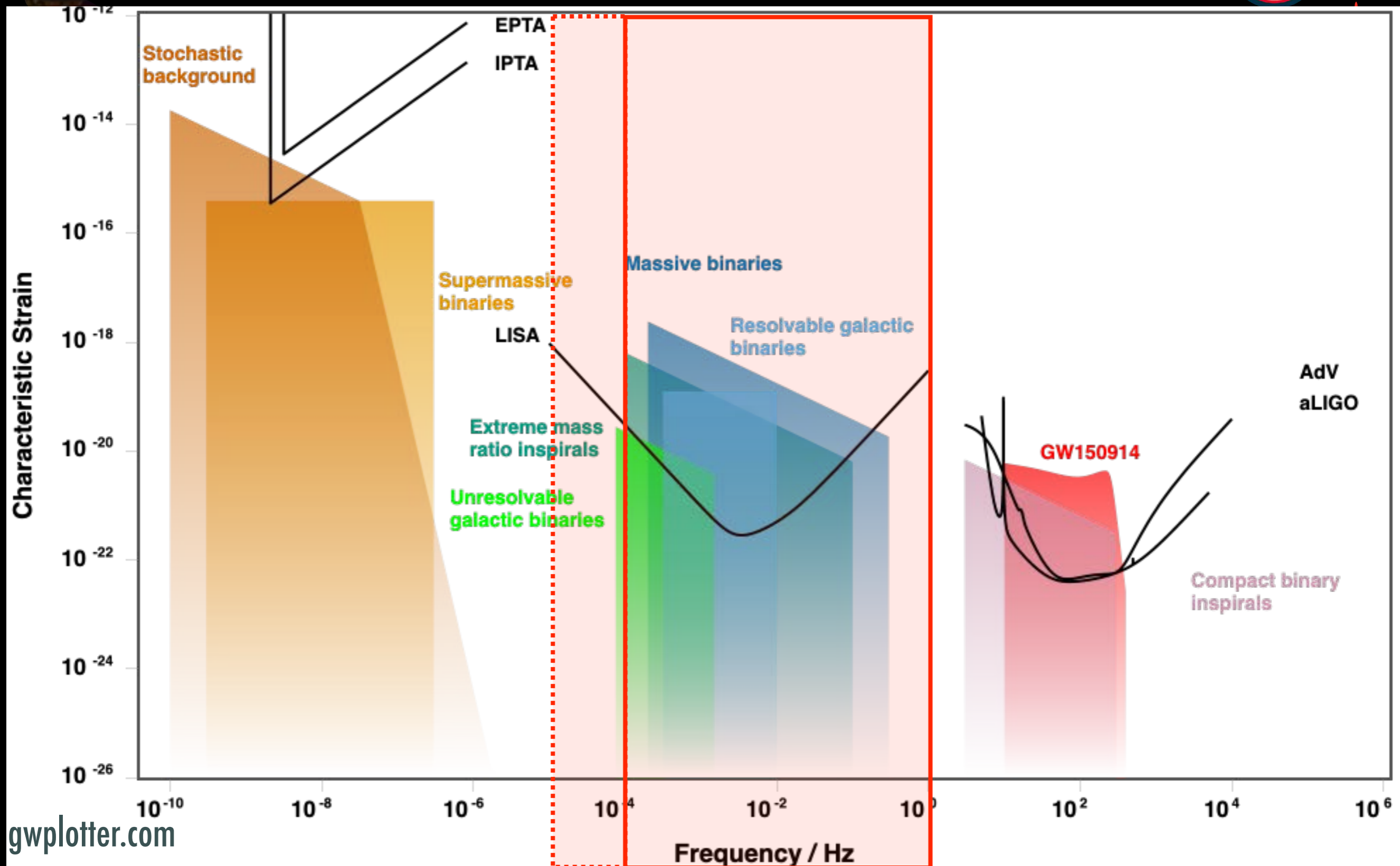


GW spectrum

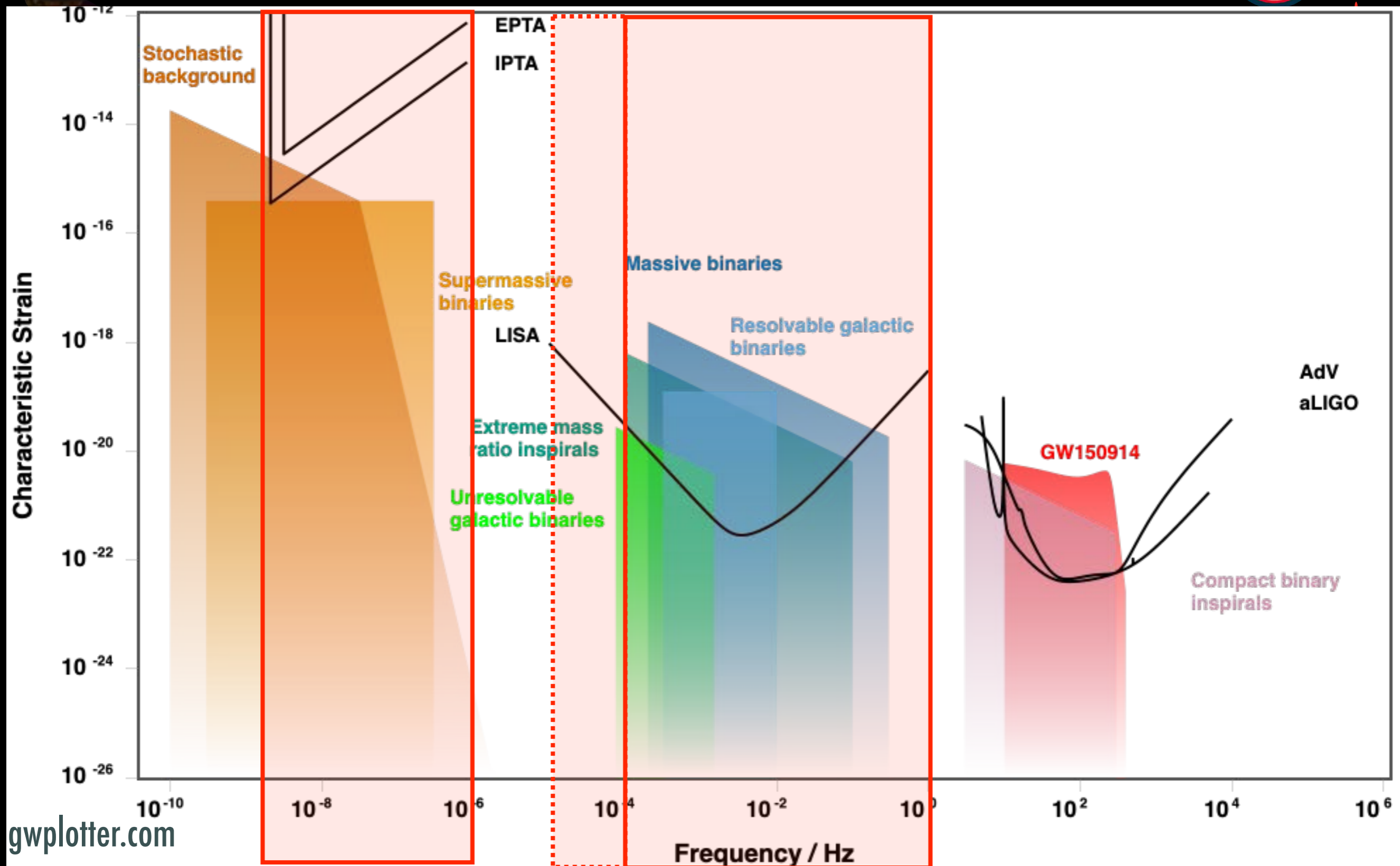


gwplotter.com

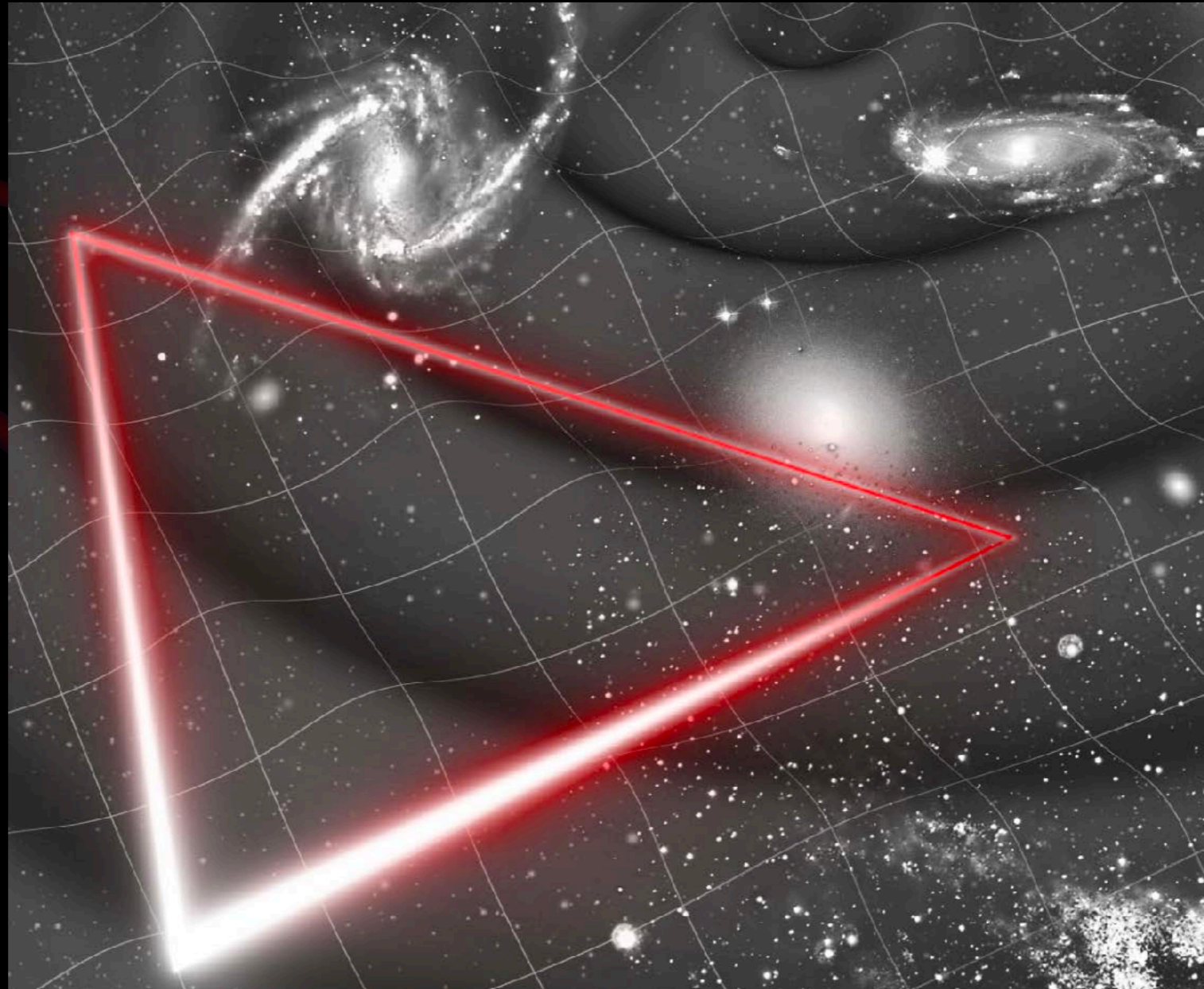
GW spectrum



GW spectrum



gwplotter.com

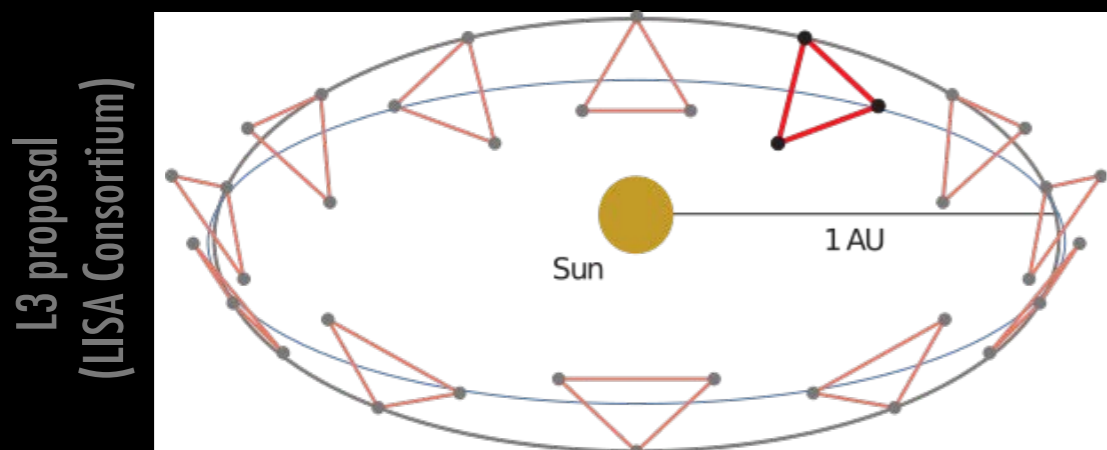
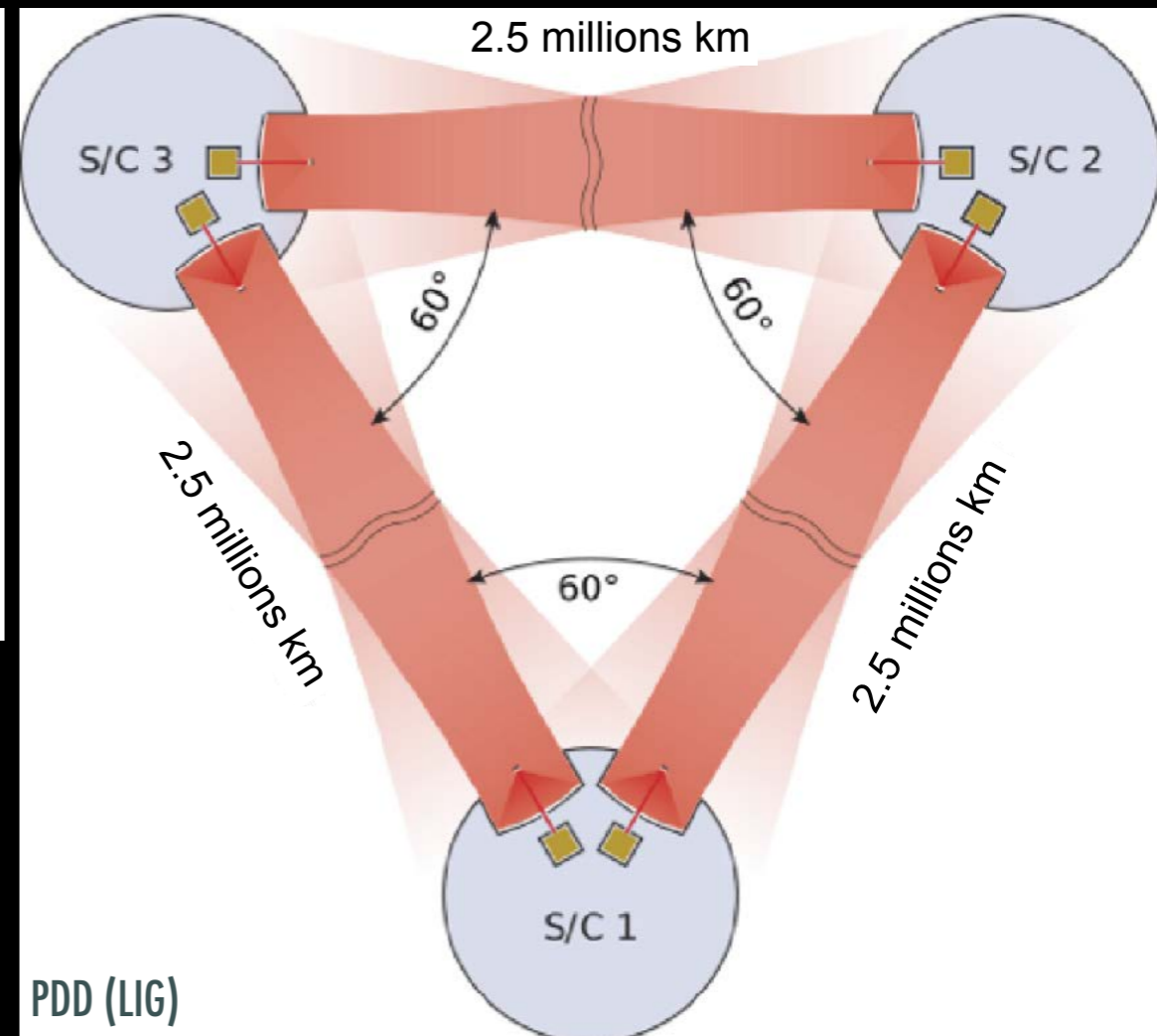
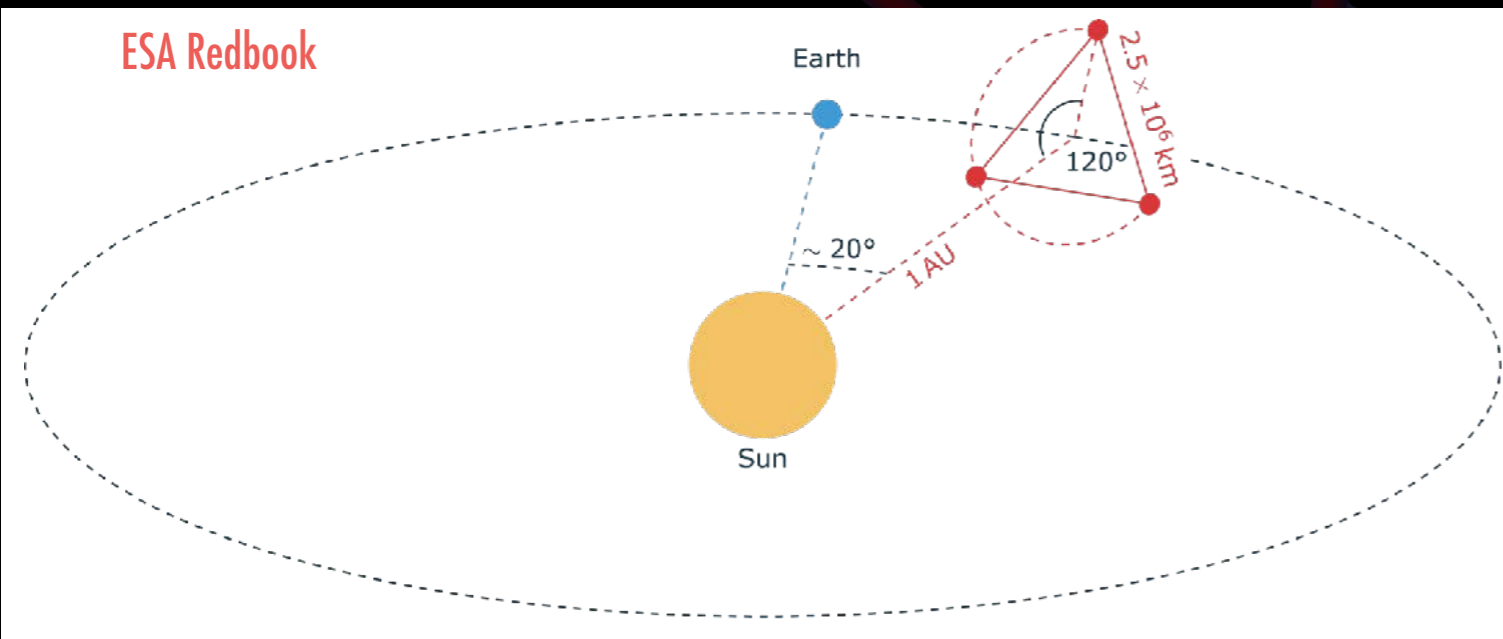


LISA

LISA



- ▶ Laser Interferometer Space Antenna
- ▶ 3 spacecrafts on heliocentric orbits separated by **2.5 millions km**
- ▶ Goal: detect strains of 10^{-21} by monitoring arm length changes at the few **picometre** level
- ▶ Sensitive only to gravity => **reference masses** protected in spacecraft
- ▶ High precision measurements => **multiple interferometers**



GW sources in the mHz band

► **Binaries:** large range of masses and mass ratios:

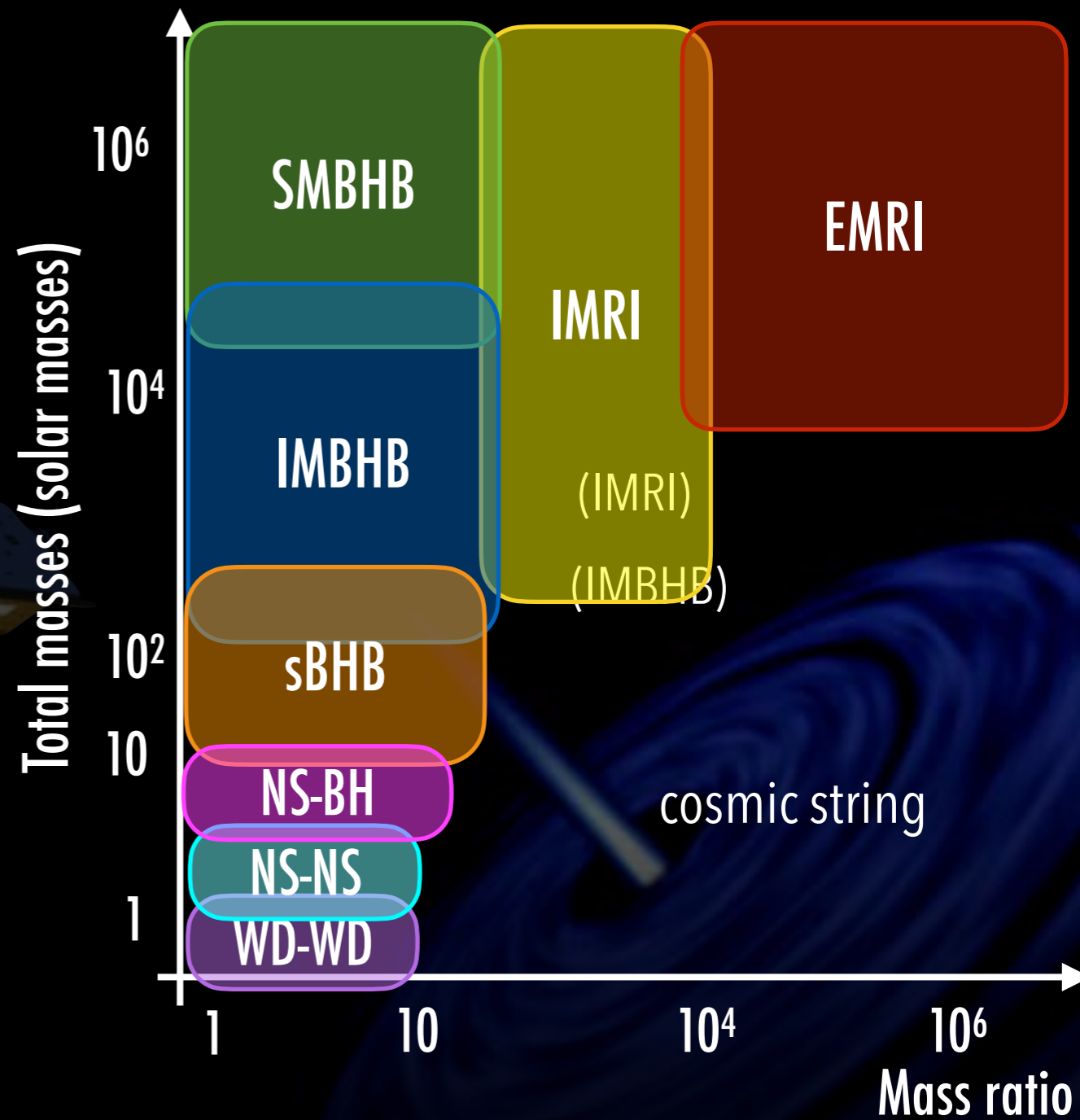
- SuperMassive BH Binaries (SMBHB)
- Extreme Mass Ratio Inspiral (EMRI)
- Stellar mass BH Binaries (sBHB)
- Double White Dwarfs (WD-WD)
- Double Neutron Stars (NS-NS)
- Intermediate Mass Ratio Inspiral
- Intermediate Mass BH Binaries

► **Stochastic backgrounds:**

- First order phase transitions, networks, ...

► Bursts: cosmic strings, ...

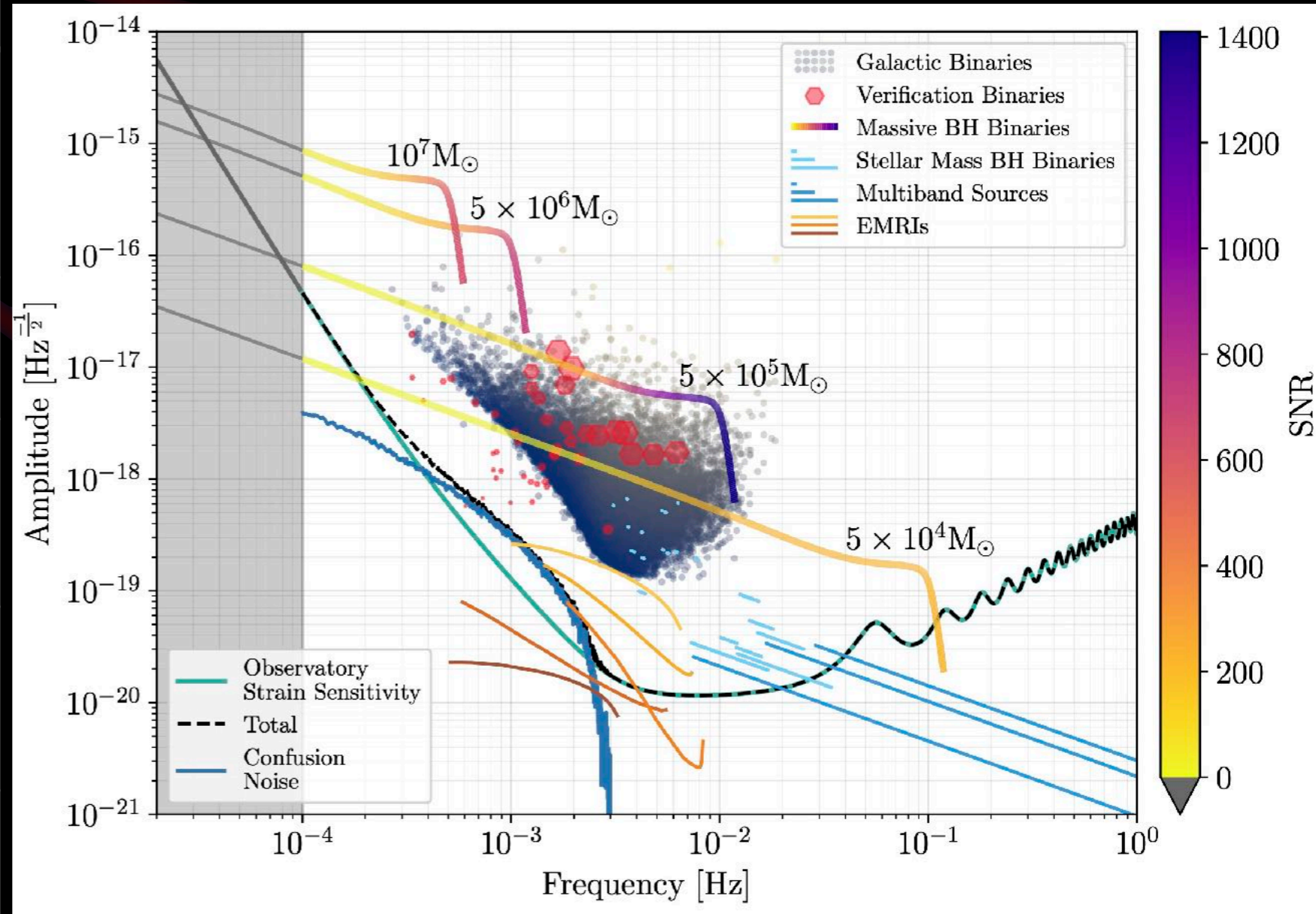
► Unknown?



Binaries observed by LISA



Sources	SNR	Duration	Event rate
Galactic binaries	10 – 500	permanent	10000 – 30000 detectables + background
Verification binaries	7 - 100	permanent	20 (today)
Stellar mass black hole binaries	7 - 30	1 à 10 years	1 to 20
Extreme Mass Ratio Inspirals	7 - 60	1 year	1 to 2000 / year
Massive Black Hole binaries	10 - 3000	Hours - months	10 to 100 / year



Science Objectives



▶ **S01:** Study the formation and evolution of **compact binary stars** in the Milky Way Galaxy.

Astrophysics

▶ **S02:** Trace the origin, growth and merger history of **massive black holes** across cosmic ages.

▶ **S03:** Probe the properties and immediate **environments of black holes** in the local Universe using **EMRIs** and **IMRIs**.

Fundamental physics

▶ **S04:** Understand the **astrophysics of stellar origin black holes**.

▶ **S05:** Explore the **fundamental nature of gravity and black holes**.

▶ **S06:** Probe the rate of **expansion** of the Universe.

▶ **S07:** Understand **stochastic GW backgrounds** and their implications for the **early Universe** and TeV-scale particle physics.

Cosmology

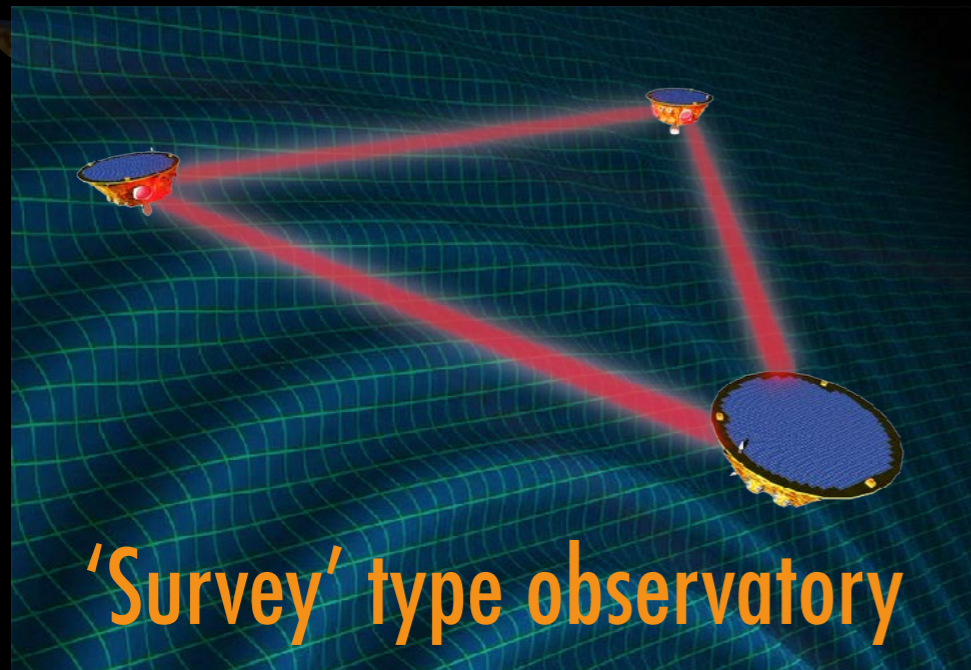
▶ **S08:** Search for GW **bursts** and **unforeseen** sources.

Data



**Gravitational wave sources
emitting between 0.02mHz
and 1 Hz**

Data



Gravitational wave sources
emitting between 0.02mHz
and 1 Hz

Data

Phasemeters (carrier, sidebands, distance)

- + DFACS* & CMD**
- + Diagnostics
- + Auxiliary channels

'Survey' type observatory

Gravitational wave sources emitting between 0.02mHz and 1 Hz

* Drag-Free Attitude Control System

** Charge Management Device

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'Survey' type observatory

Calibrations corrections
 + Resynchronisation (clock)
 + Time-Delay Interferometry
 reduction of laser noise

Gravitational wave sources emitting between 0.02mHz and 1 Hz

3 TDI channels with 2 " ~independents"

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Data Analysis of GWs

Catalogs of GWs sources with their waveform

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L0

L0.5

L1

L2

L3



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Data Analysis of GWs

Catalogs of GWs sources with their waveform

Data

Mission Operation Center (ESA)

Science Operation Center (ESA)

DDPC: Distributed Data Processing Center (ESA Member States)

NASA Ground Segment

Phasemeters (carrier, ... ds, distance)
 CS* & CMD**
 + Diagnostics
 + Auxiliary channels



L0

L0.5

Calibrations corrections
 + Resynchronisation (clock)
 + **Time-Delay Interferometry**
 reduction of laser noise

L1 3 TDI channels with 2 " ~independents"

L2 Data Analysis of GWs

L3 Catalogs of GWs sources with their waveform

Data Analysis

- ▶ Analysis of **all signals** and **noises** together
=> **global analysis**
- ▶ **Flexibility**: first data of this kind challenge:
 - Multiple approaches, multiple pipelines
 - Quick development from prototyping to production
- ▶ **General approach** with with multiple iterative (interconnection between products):
 1. Reduce dominant noises (Time Delay Interferometry) and partial correction on instrument artefacts => L1 data (TDI data)
 2. **GLOBAL FITS**: GW sources extraction + better understanding of noises and instrument with multiple pipelines => L2 data
 3. Cross-check, combination, merging of L2 data to produce catalogs + associated scientific products => L3 data
- ▶ **Distributed Data Computing Center (DDPC)**



LISA Data analysis



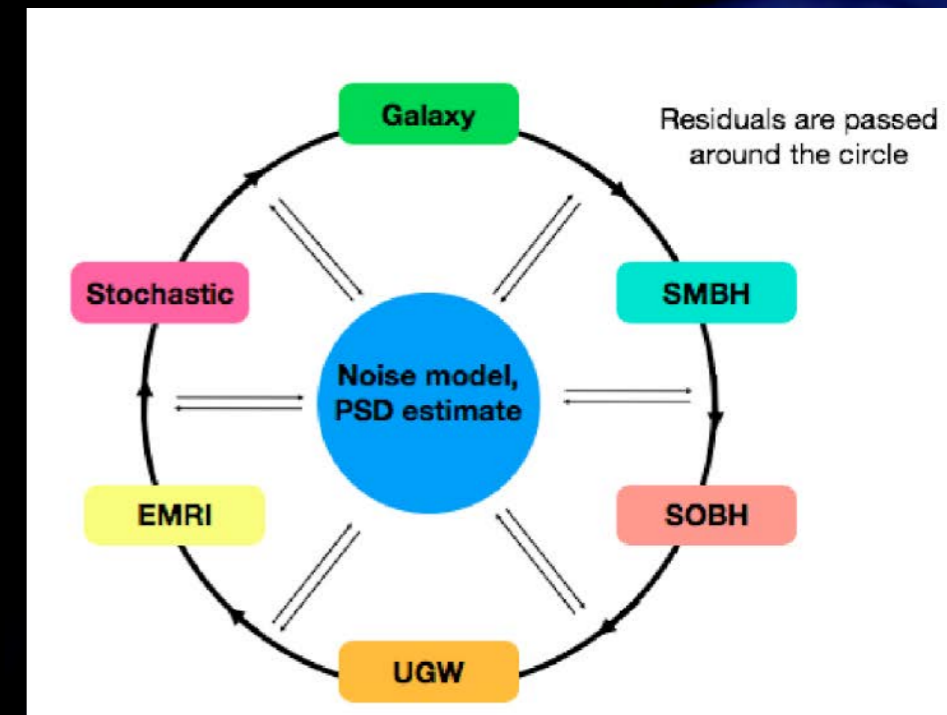
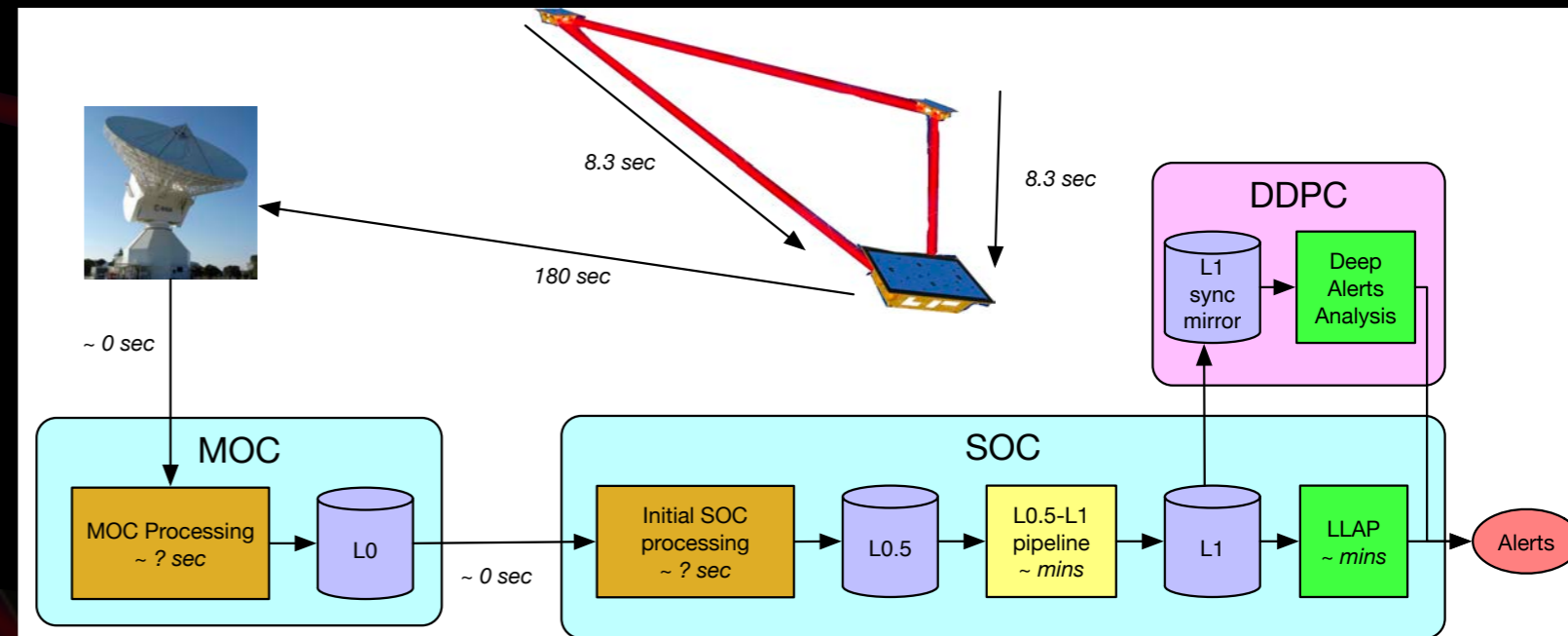
▶ Low Latency Alert Pipeline:

- Fast and online
- Multiple approaches/pipelines in parallel

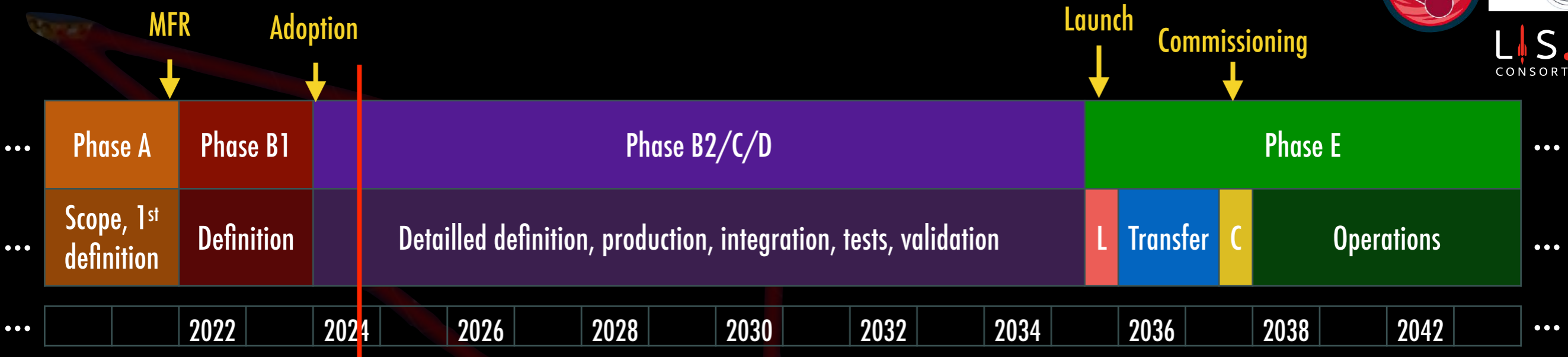
▶ Deep Analysis:

multiple global fits:

- Large number of parameters
- Disentangle sources
- Several timescale for the analysis depending on sources
- Current approaches in the prototypes:
 - Bayesian analysis, matched filtering;
 - Start to use some AI;
 - Others approaches (sparsity, ...).
- Cost for one global fit ~ 200 millions cpu.h per year



LISA now



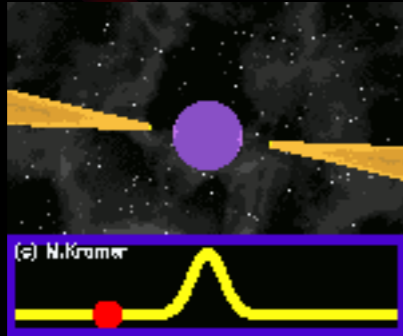
- ▶ Adopted in January 2024 : ressources available, building started
- ▶ Launch in 2035
- ▶ **Distributed Data Processing Center:**
 - Led by France
 - Activities are really starting now
 - Simulation tools and simulated datasets
 - Many available prototypes of data analysis pipelines



Pulsar Timing Array

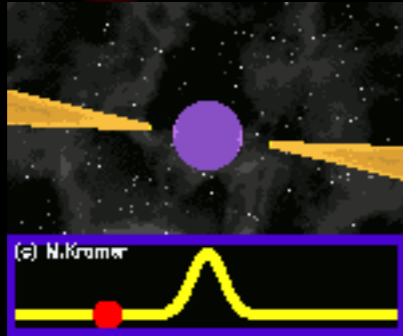
Pulsar timing

- ▶ Precise timing of arrival time of pulses => Time Of Arrival (TOA)



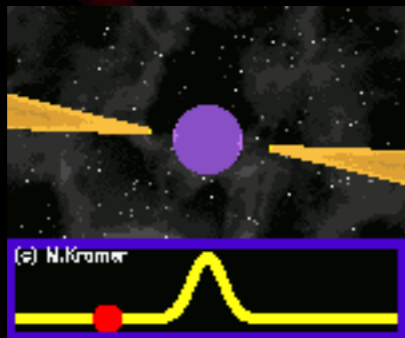
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Radiotelescope

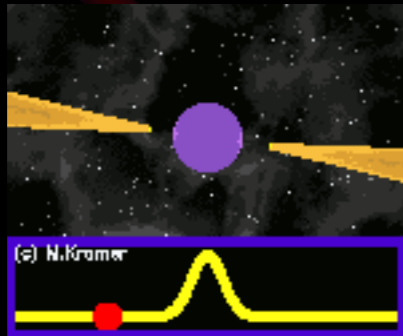


Receiver (GHz)



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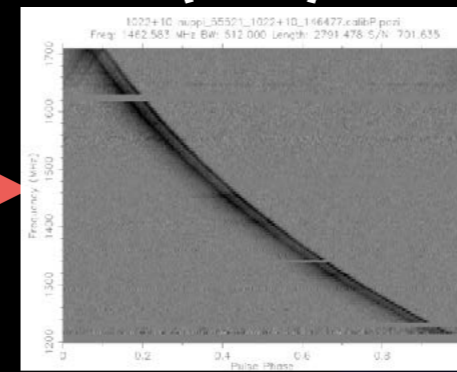
Radiotelescope



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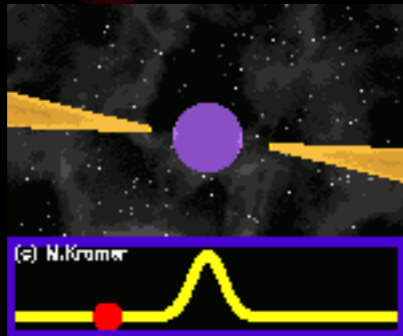


Coherent dedispersion (GPU)



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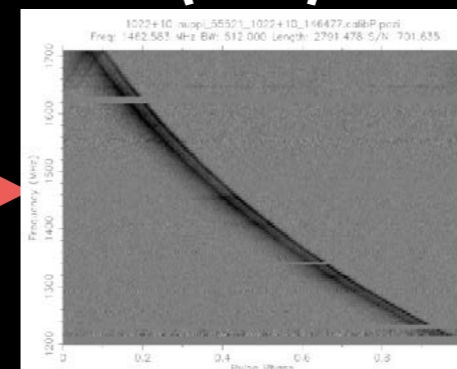
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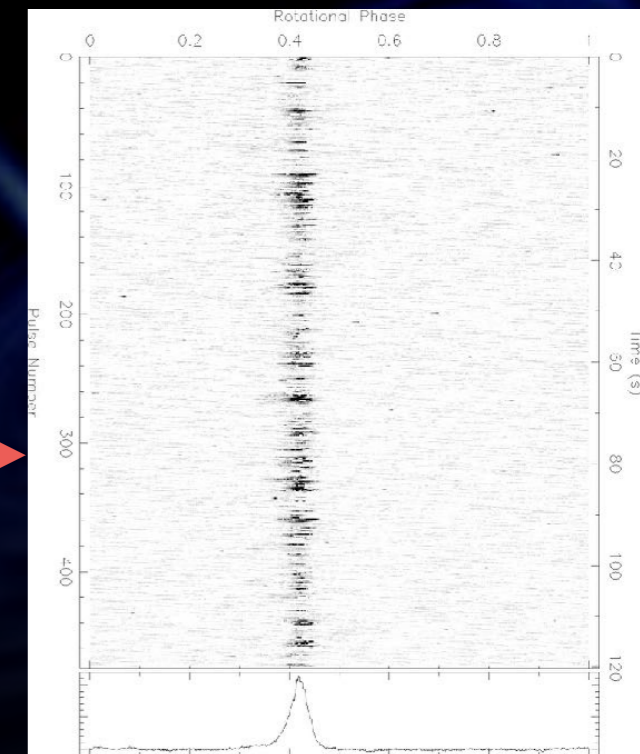
Receiver (GHz)



Coherent dedispersion (GPU)



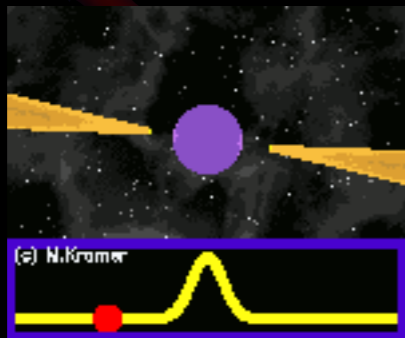
Folding



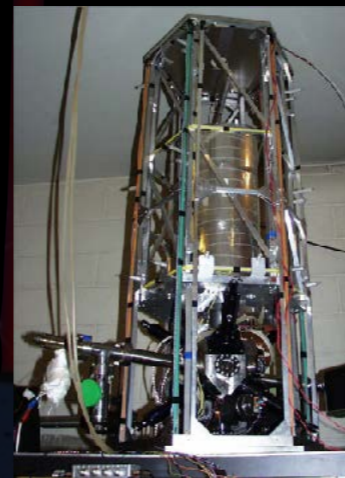
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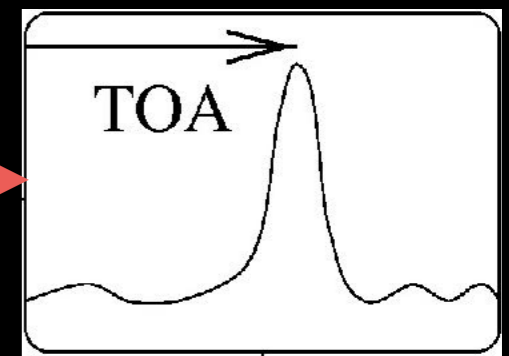
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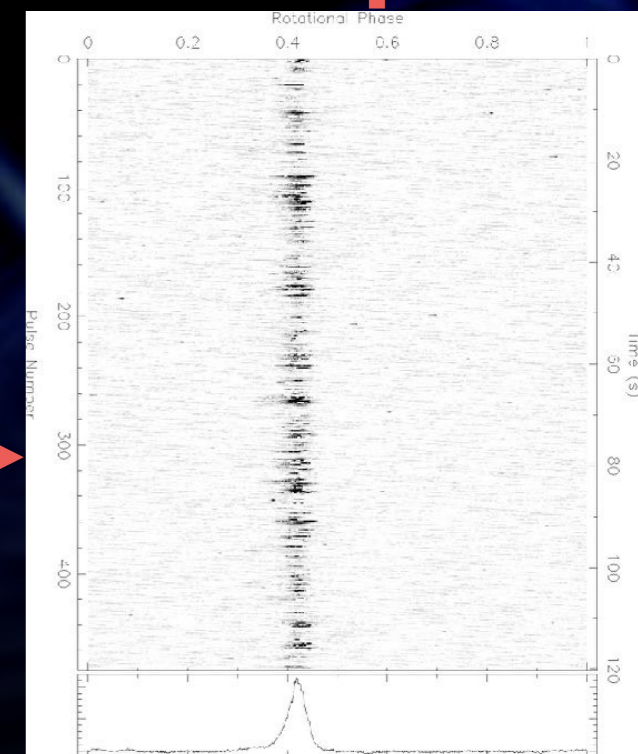
Reference clock



Integrated pulse



Folding



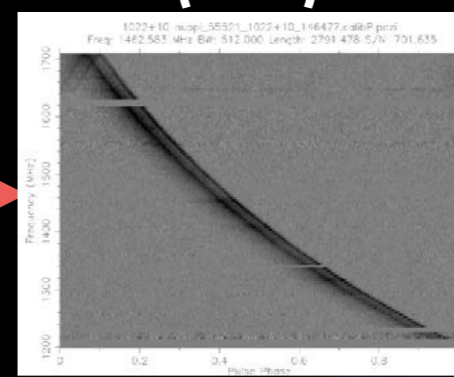
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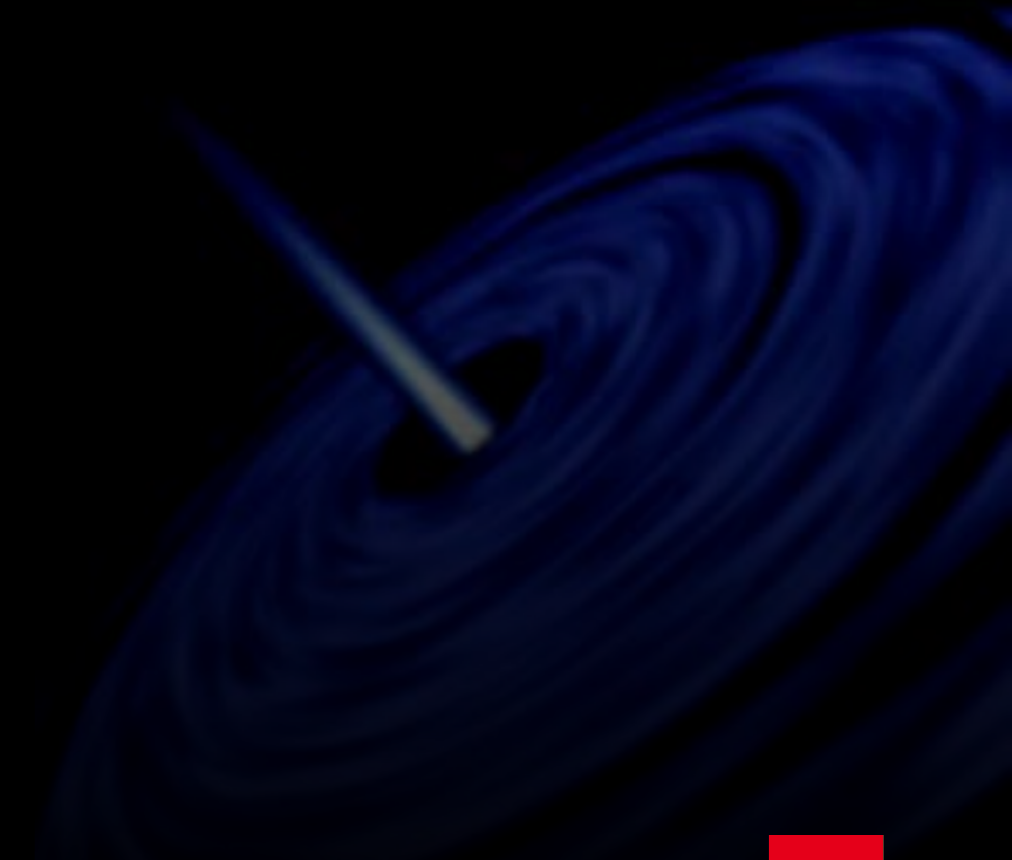
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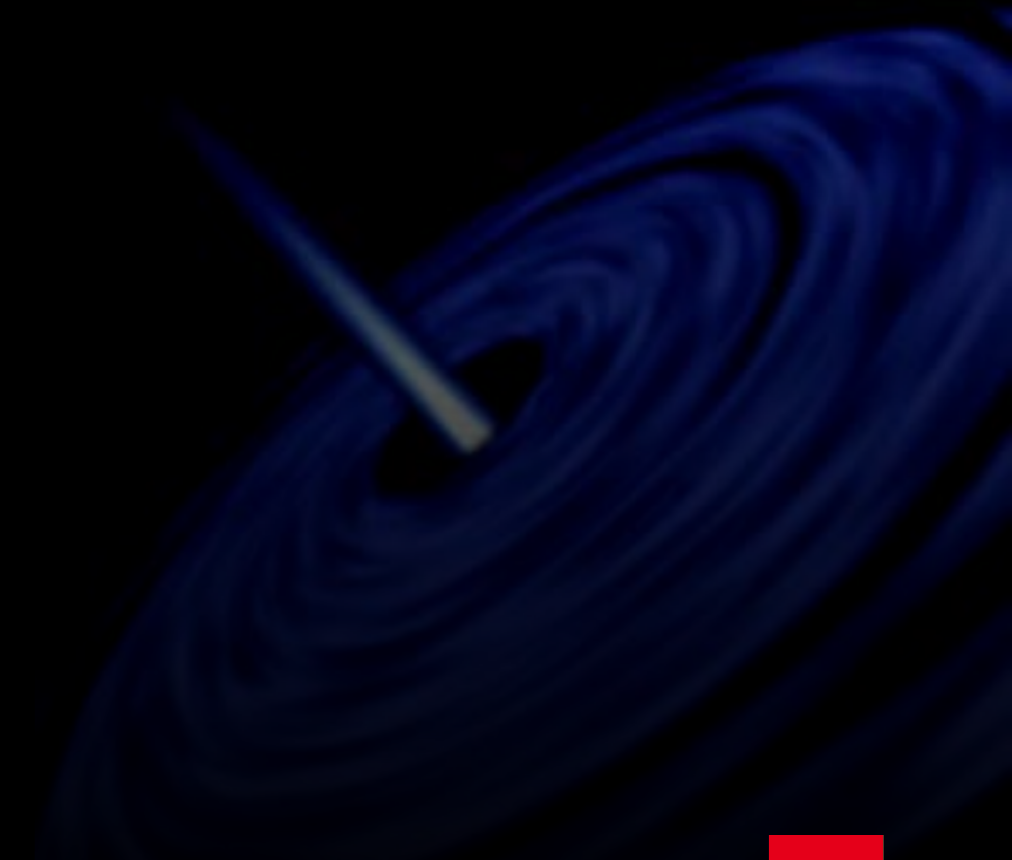
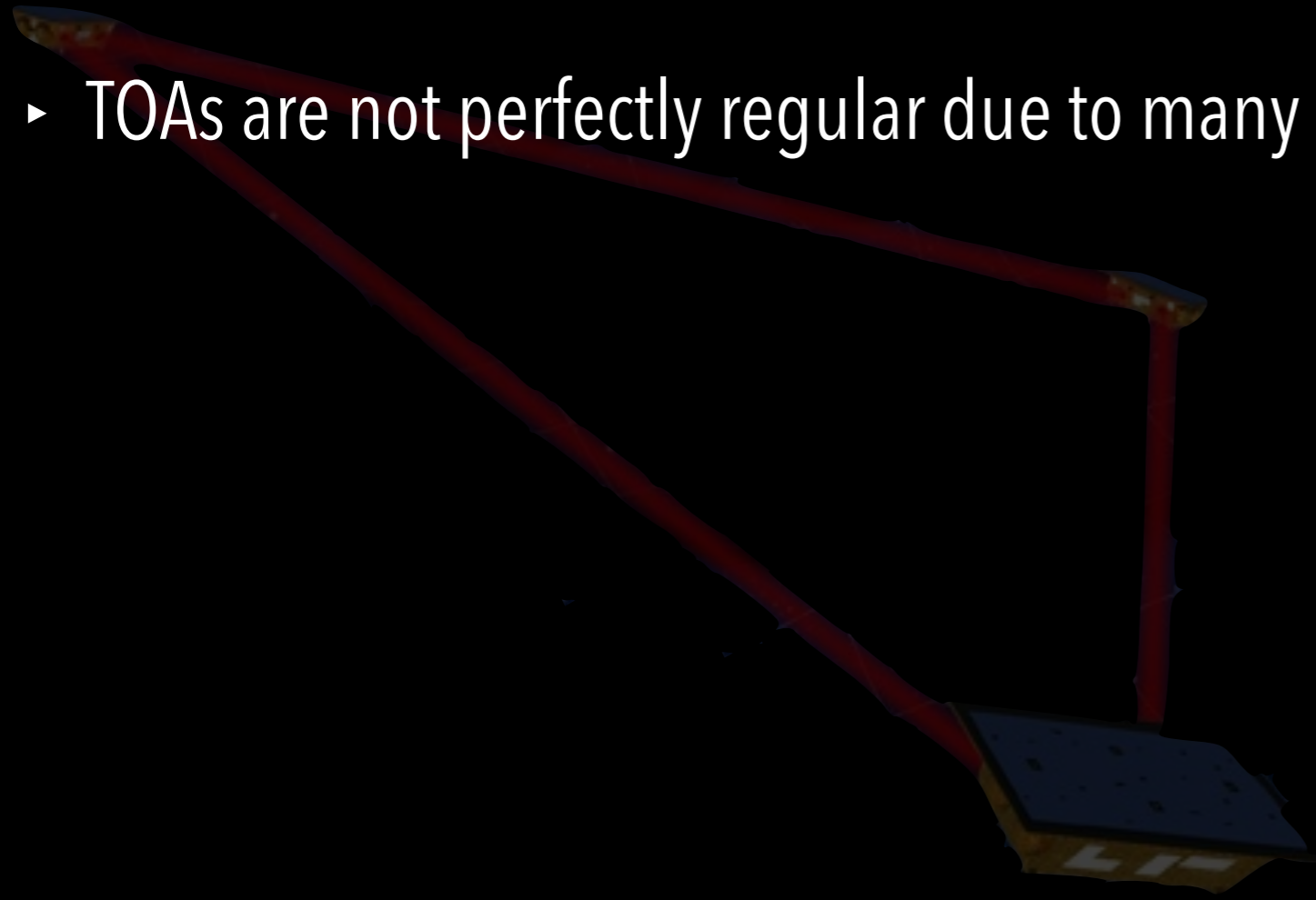


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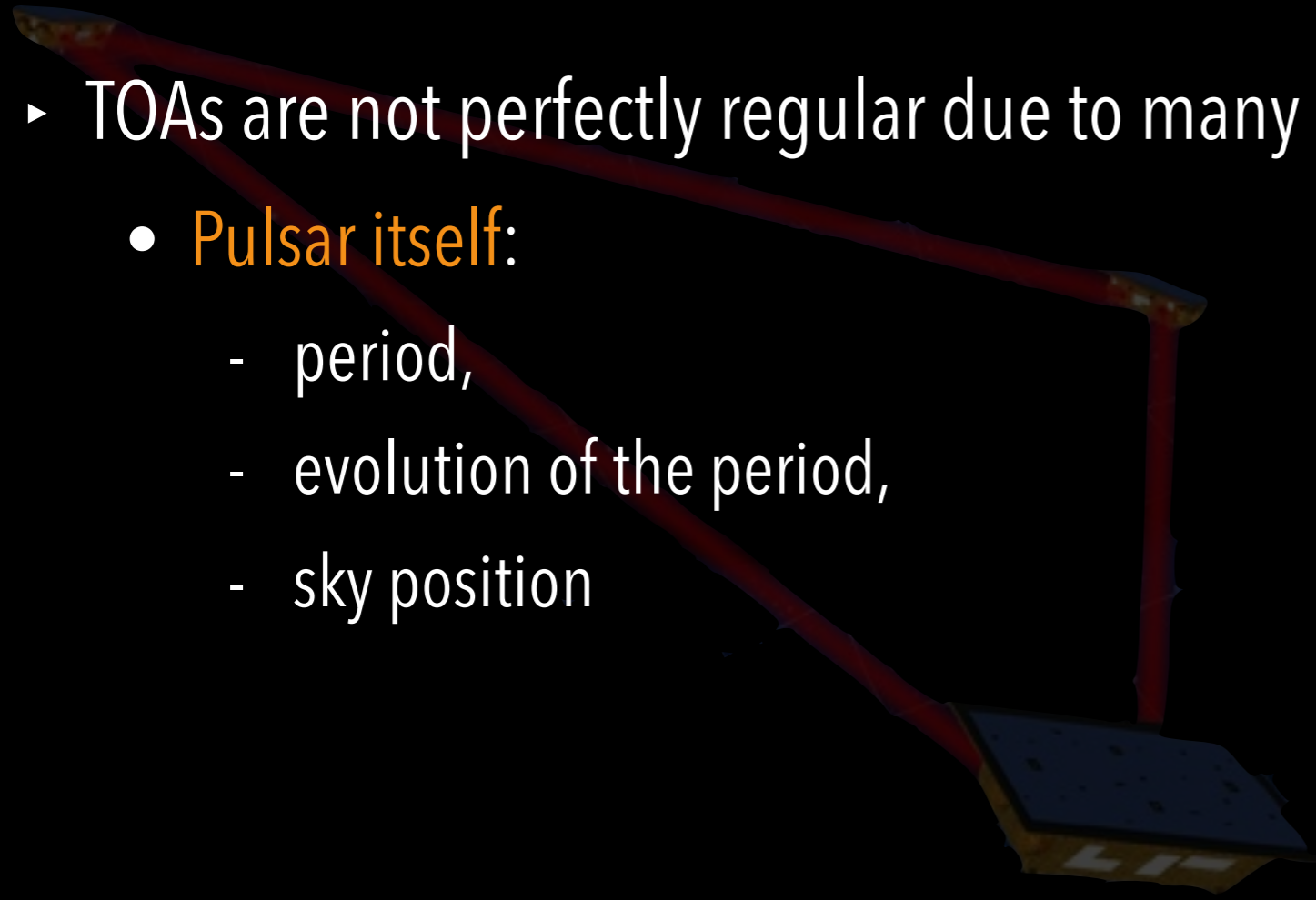
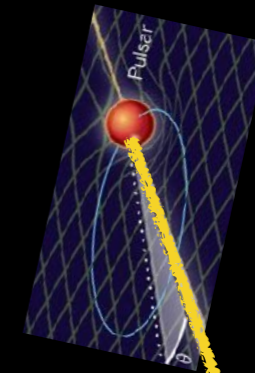
Pulsar timing

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Pulsar timing

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 - Pulsar itself:
 - period,
 - evolution of the period,
 - sky position



Pulsar timing

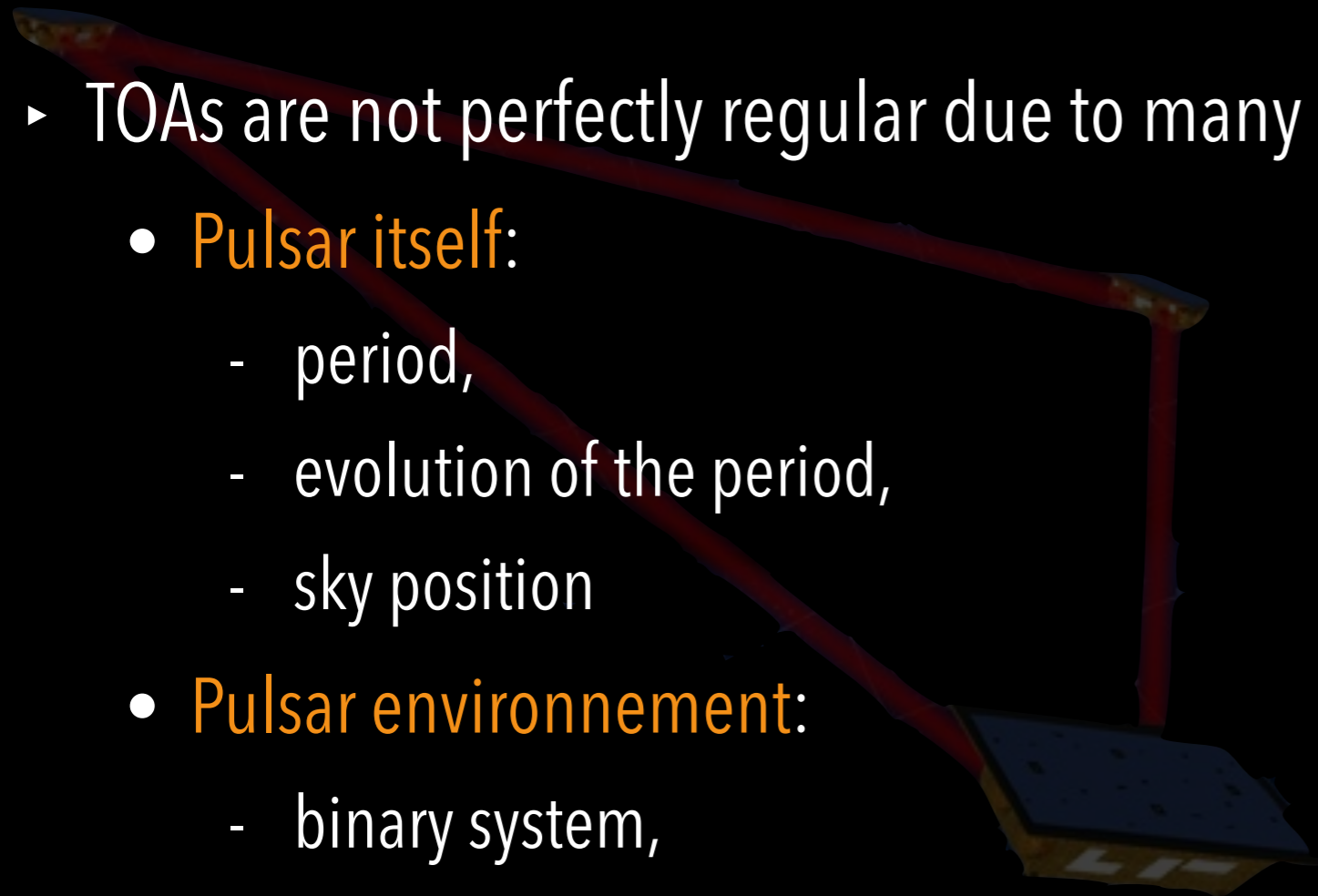
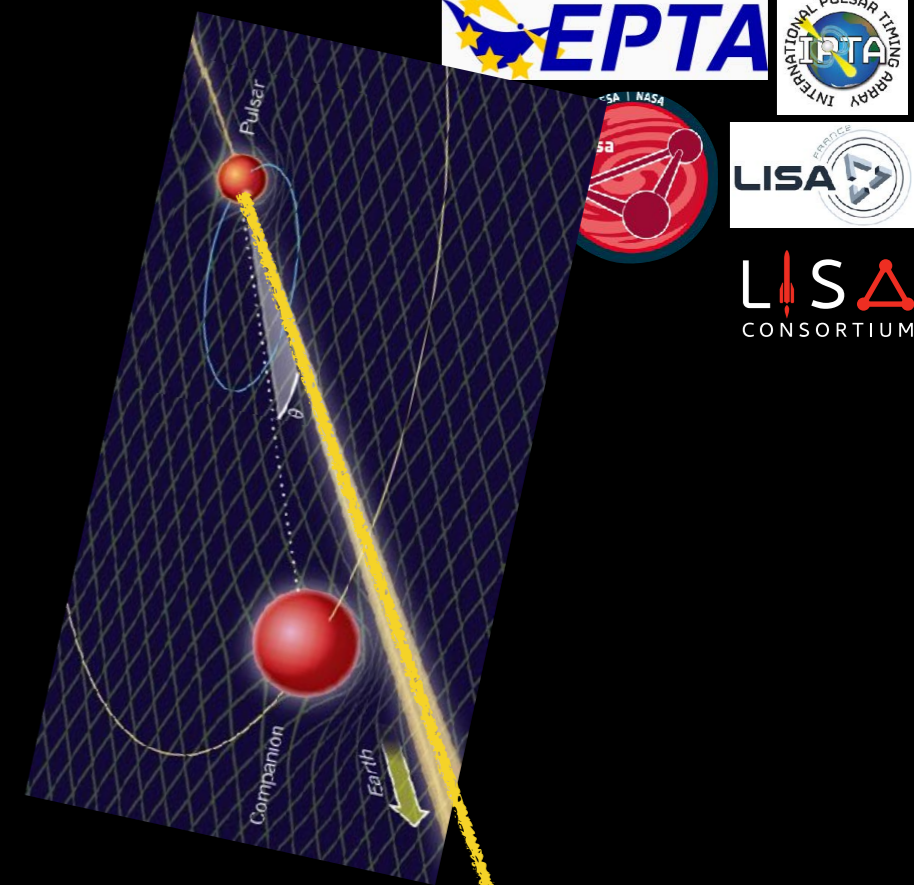
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- Pulsar environment:

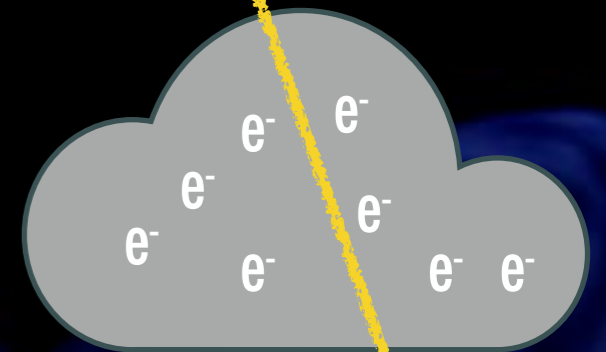
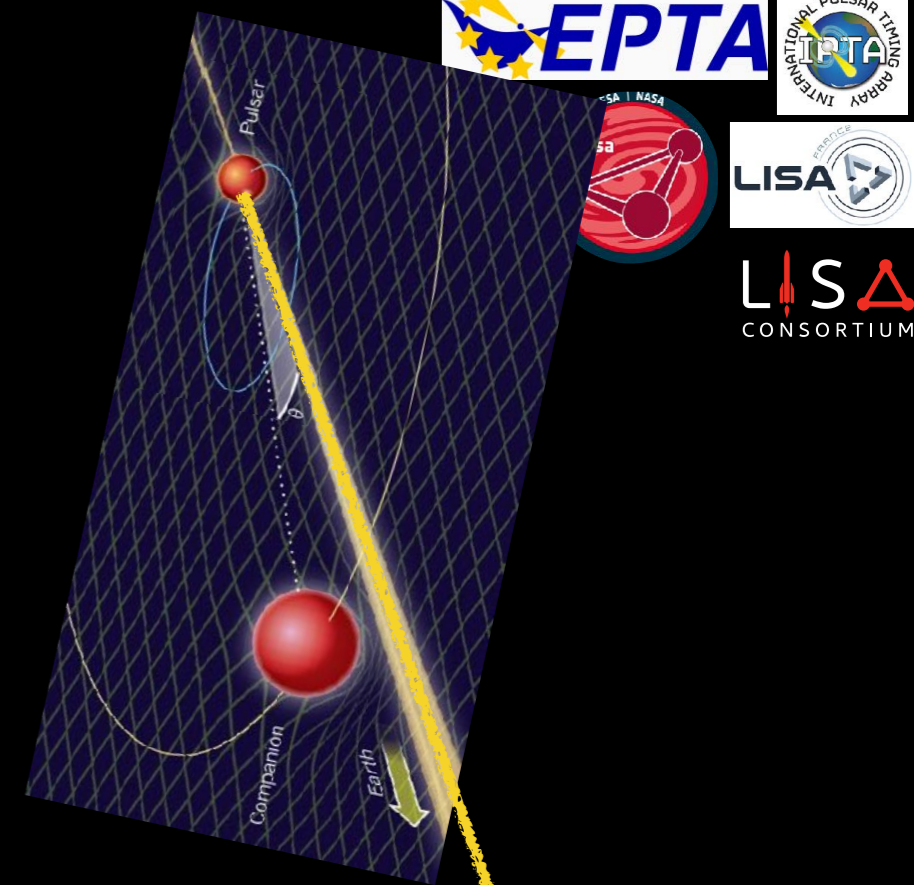
- binary system,
- proper motion



Pulsar timing

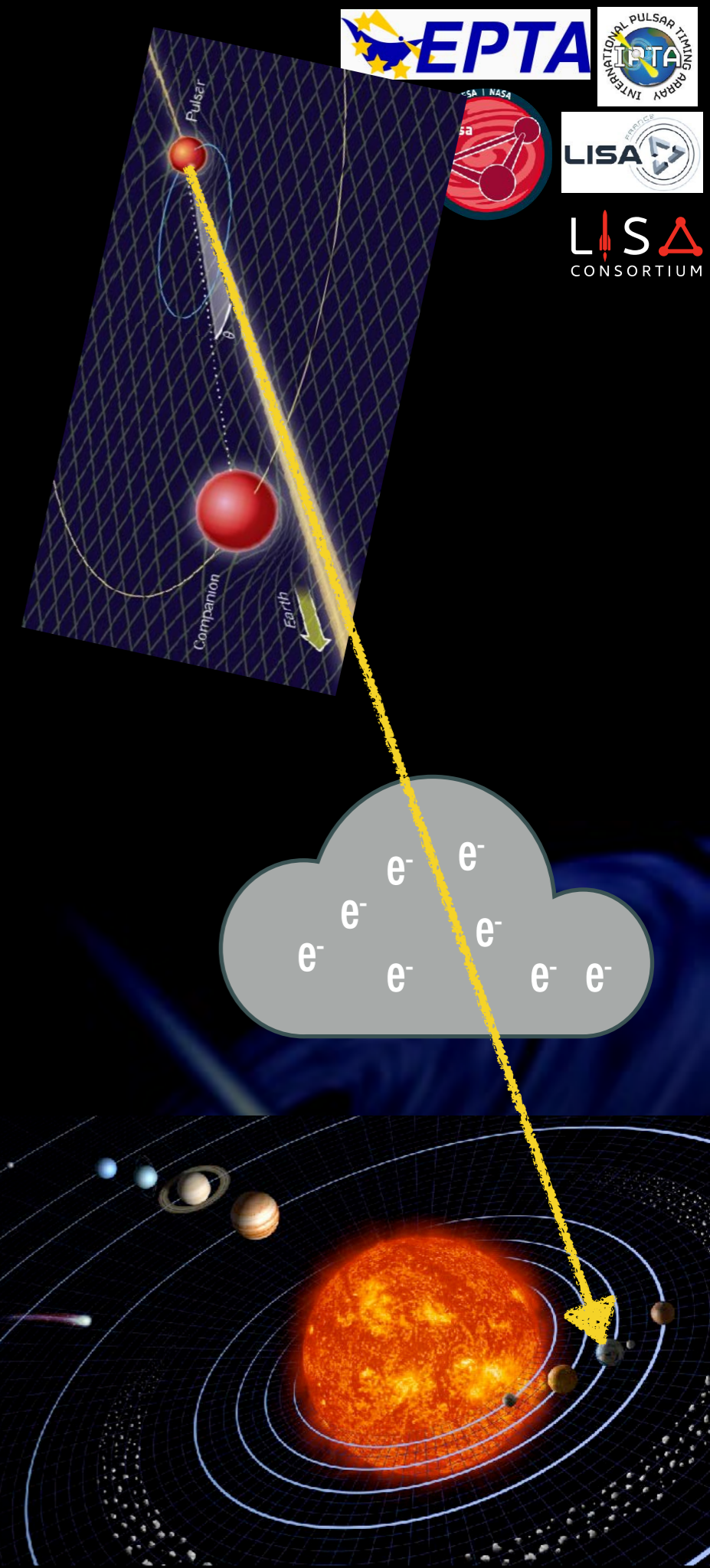
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- **Beam propagation:** interstellar medium



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 - **Earth position** (ephemerides of the Solar System)



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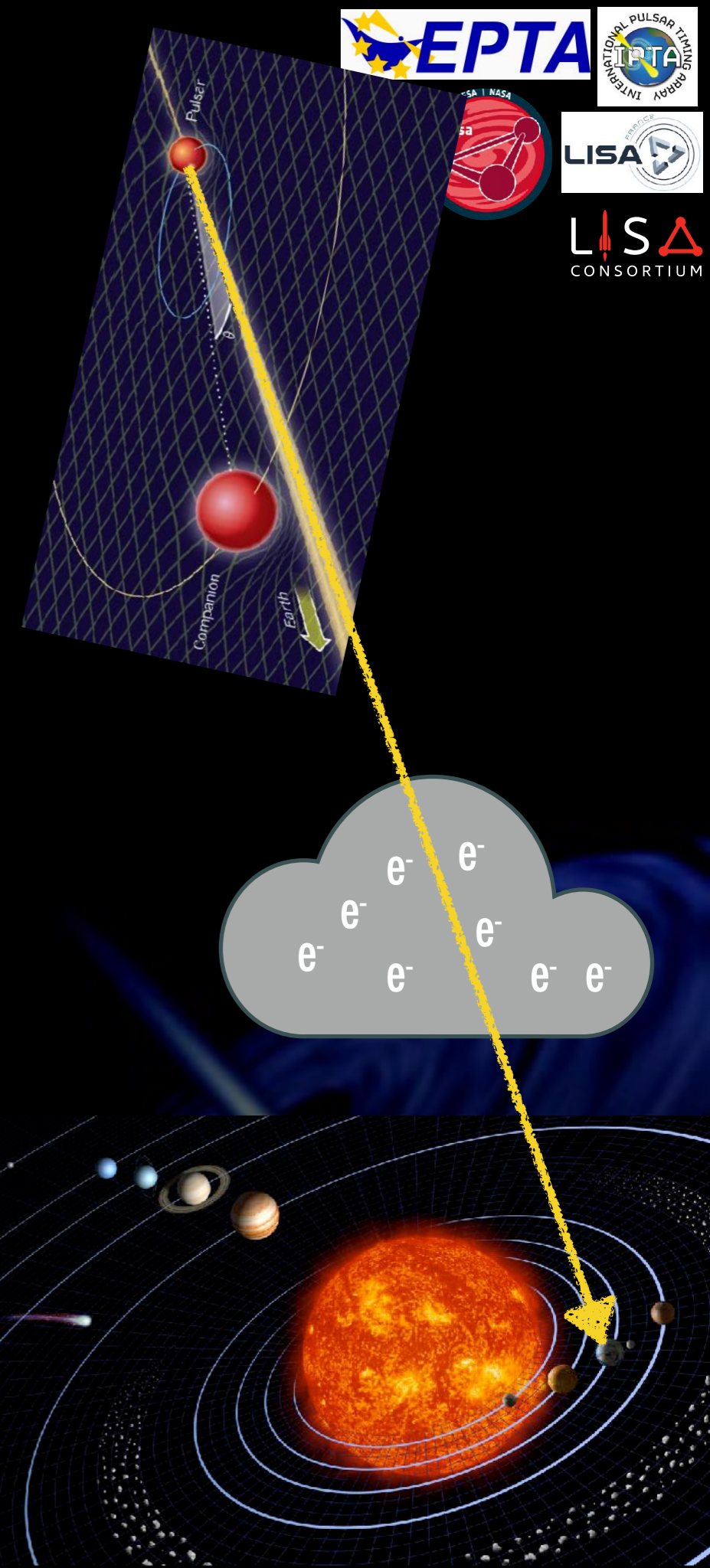
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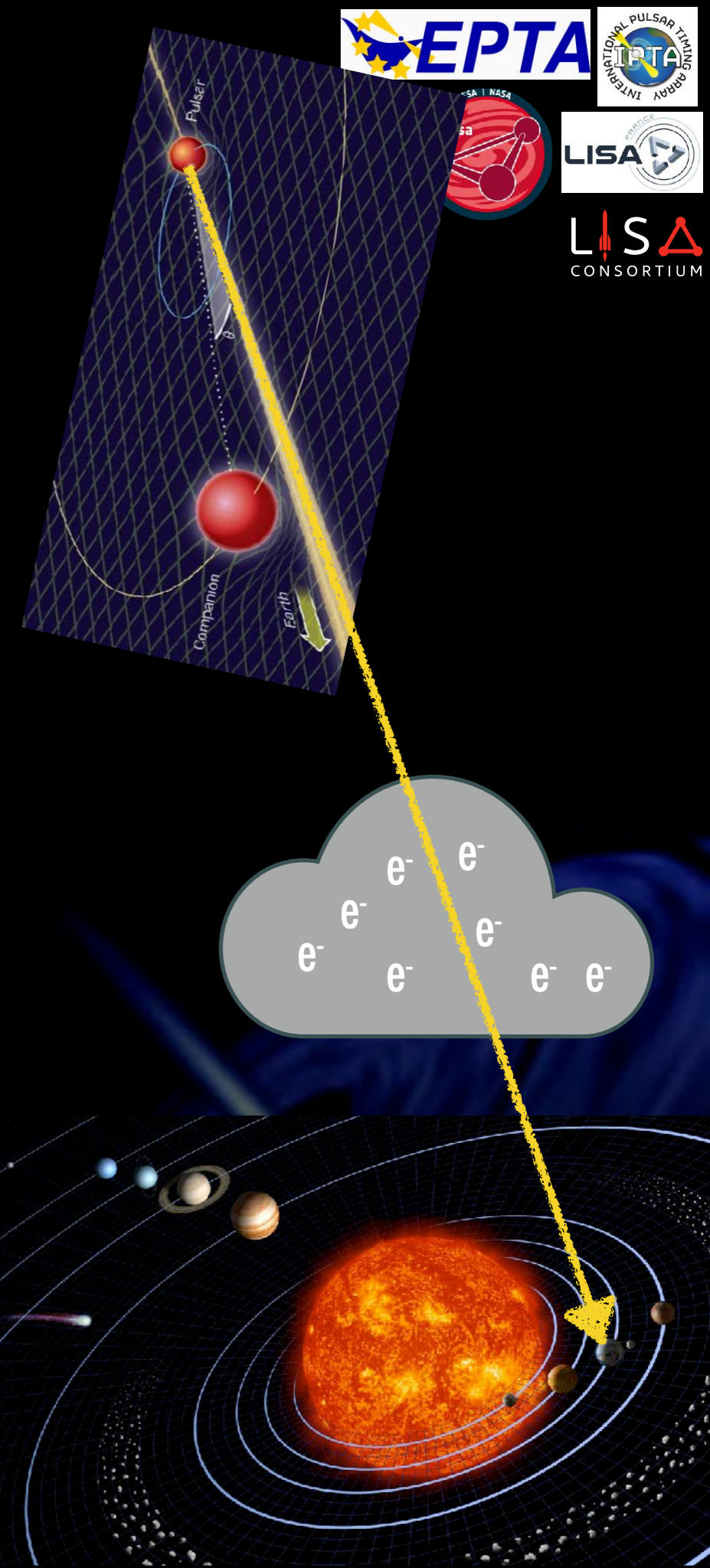
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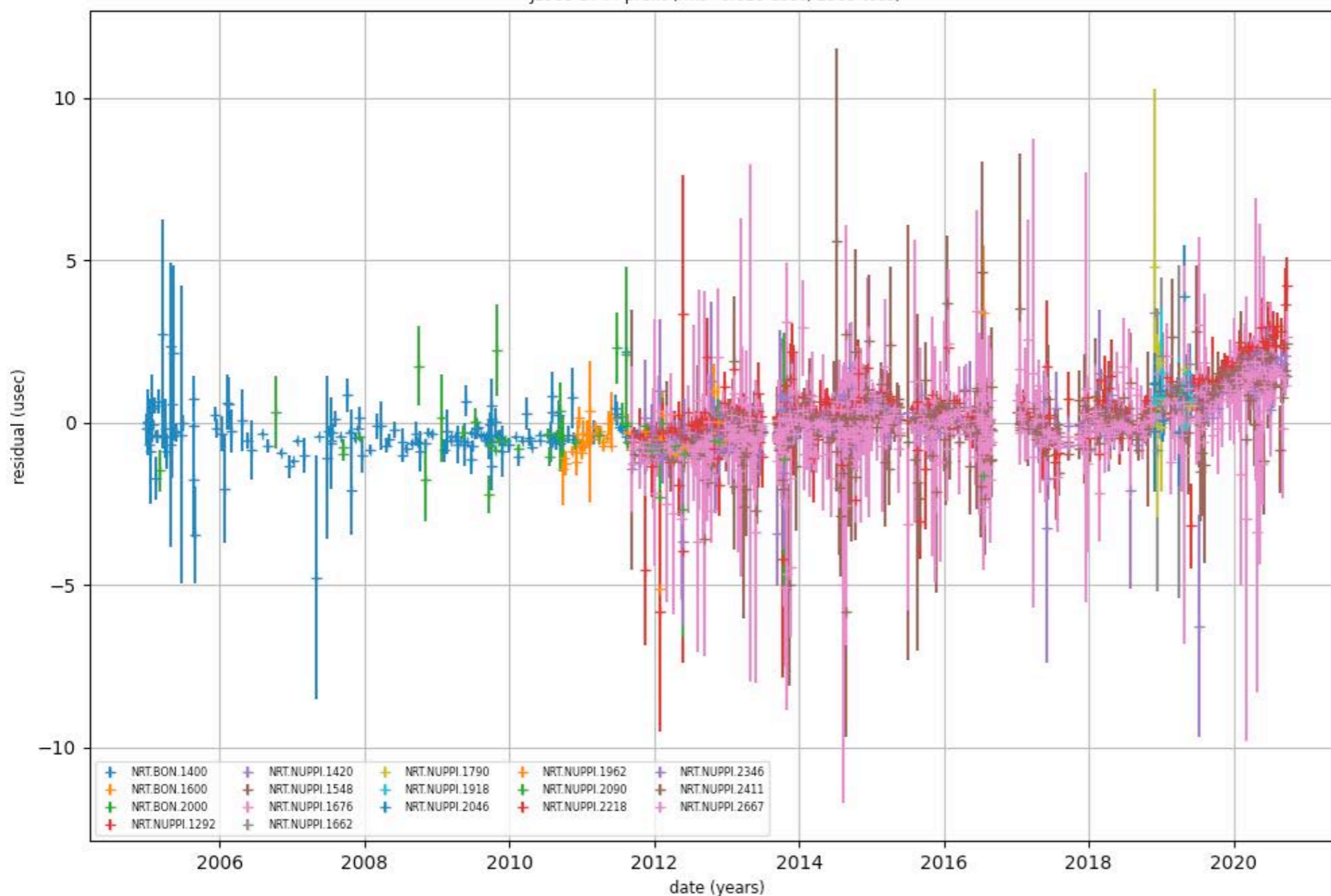
▶ Modelling of each pulsars



Pulsar timing

- ▶ Examples:
 - J1909-3744:

J1909-3744 prefit (rms=0.629 usec, 2503 toas)



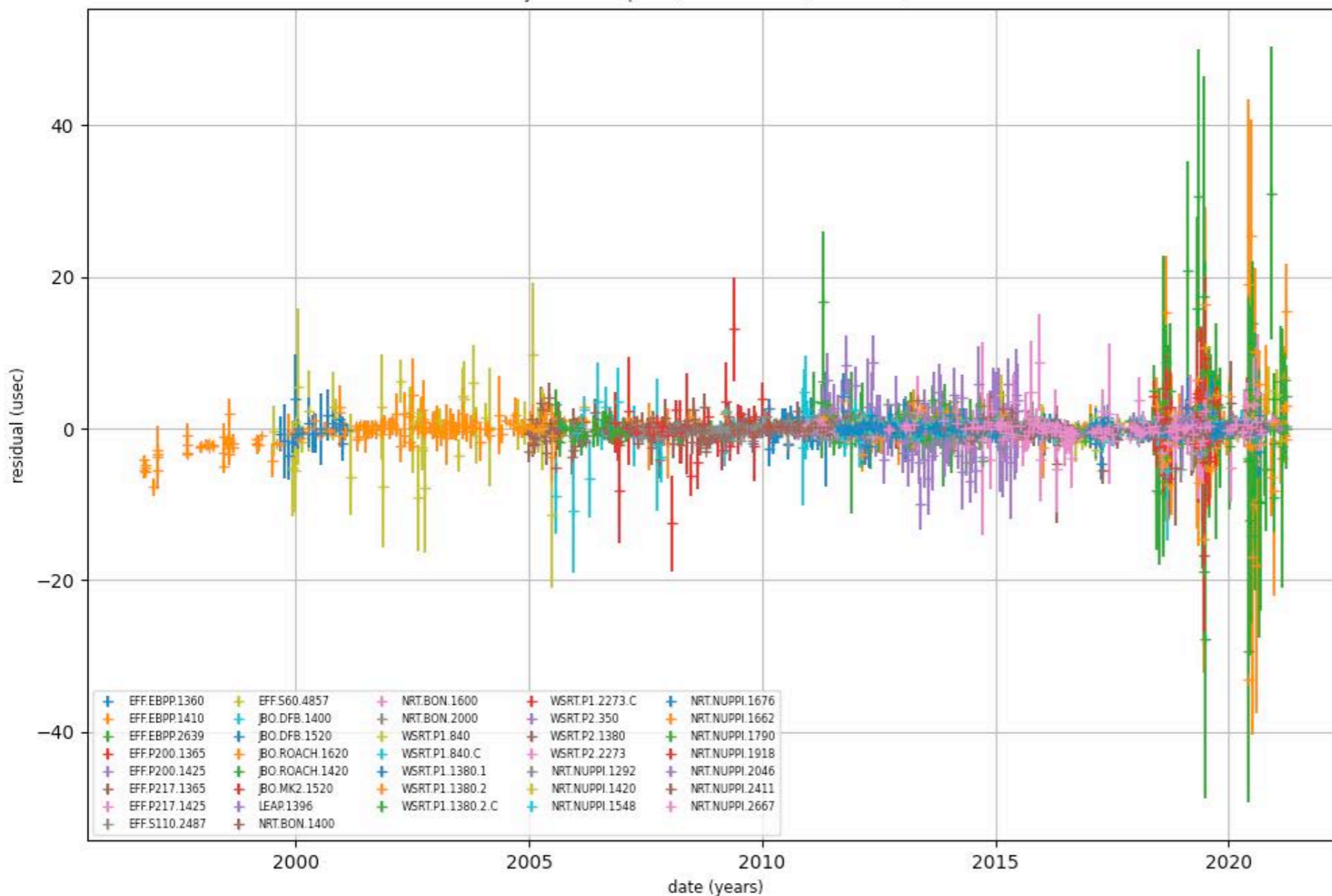
Name	fit	prefit
RAJ	yes	5.01691 +/- 5.01691
DECJ	yes	-0.658641 +/- -0.658641
F0	yes	339.316 +/- 339.316
F1	yes	-1.6148e-15 +/- -1.6148e-15
DM	yes	10.3906 +/- 10.3906
DM1	yes	-0.000250904 +/- -0.000250904
DM2	yes	1.48176e-05 +/- 1.48176e-05
PMRA	yes	-9.52683 +/- -9.52683
PMDEC	yes	-35.8098 +/- -35.8098
PX	yes	1.0623 +/- 1.0623
SINI	yes	0.997779 +/- 0.997779
PB	yes	1.53345 +/- 1.53345
A1	yes	1.89799 +/- 1.89799
PBDOT	yes	5.1216e-13 +/- 5.1216e-13
XDOT	yes	-1.17023e-15 +/- -1.17023e-15
TASC	yes	53114 +/- 53114
EPS1	yes	4.93407e-09 +/- 4.93407e-09
EPS2	yes	-1.37334e-07 +/- -1.37334e-07
M2	yes	0.218395 +/- 0.218395
JUMP1	yes	-8.5495e-05 +/- -8.5495e-05
JUMP2	yes	-8.49454e-05 +/- -8.49454e-05
JUMP3	yes	-8.34176e-05 +/- -8.34176e-05
JUMP4	yes	-7.4828e-07 +/- -7.4828e-07
JUMP6	yes	2.58546e-07 +/- 2.58546e-07

Pulsar timing



- ▶ Examples:
 - J1713+0747:

J1713+0747 prefit (rms=0.253 usec, 5003 toas)



Name	fit	prefit
RAJ	yes	4.51091 +/- 4.51091
DECJ	yes	0.136027 +/- 0.136027
F0	yes	218.812 +/- 218.812
F1	yes	-4.08396e-16 +/- -4.08396e-16
DM	yes	15.9926 +/- 15.9926
DM1	yes	1.42664e-05 +/- 1.42664e-05
DM2	yes	-9.12919e-06 +/- -9.12919e-06
PMRA	yes	4.92273 +/- 4.92273
PMDEC	yes	-3.91239 +/- -3.91239
PX	yes	0.92902 +/- 0.92902
PB	yes	67.8251 +/- 67.8251
T0	yes	48742 +/- 48742
A1	yes	32.3424 +/- 32.3424
OM	yes	176.21 +/- 176.21
ECC	yes	7.49383e-05 +/- 7.49383e-05
PBDOT	yes	7.11226e-13 +/- 7.11226e-13
M2	yes	0.396039 +/- 0.396039
KOM	yes	99.0463 +/- 99.0463
KIN	yes	66.9501 +/- 66.9501
JUMP1	yes	0.000593315 +/- 0.000593315
JUMP2	yes	0.000592716 +/- 0.000592716
JUMP3	yes	0.000593452 +/- 0.000593452
JUMP4	yes	0.000619147 +/- 0.000619147

Pulsar noises

<https://arxiv.org/abs/2306.16225>

▶ White noise :

- $\sigma_{\text{scaled}}^2 = \text{EFAC}^2 \times \sigma_{\text{original}}^2 + \text{EQUAD}^2$. with $\sigma_{\text{original}}^2$ the original errorbars

▶ Red noises:

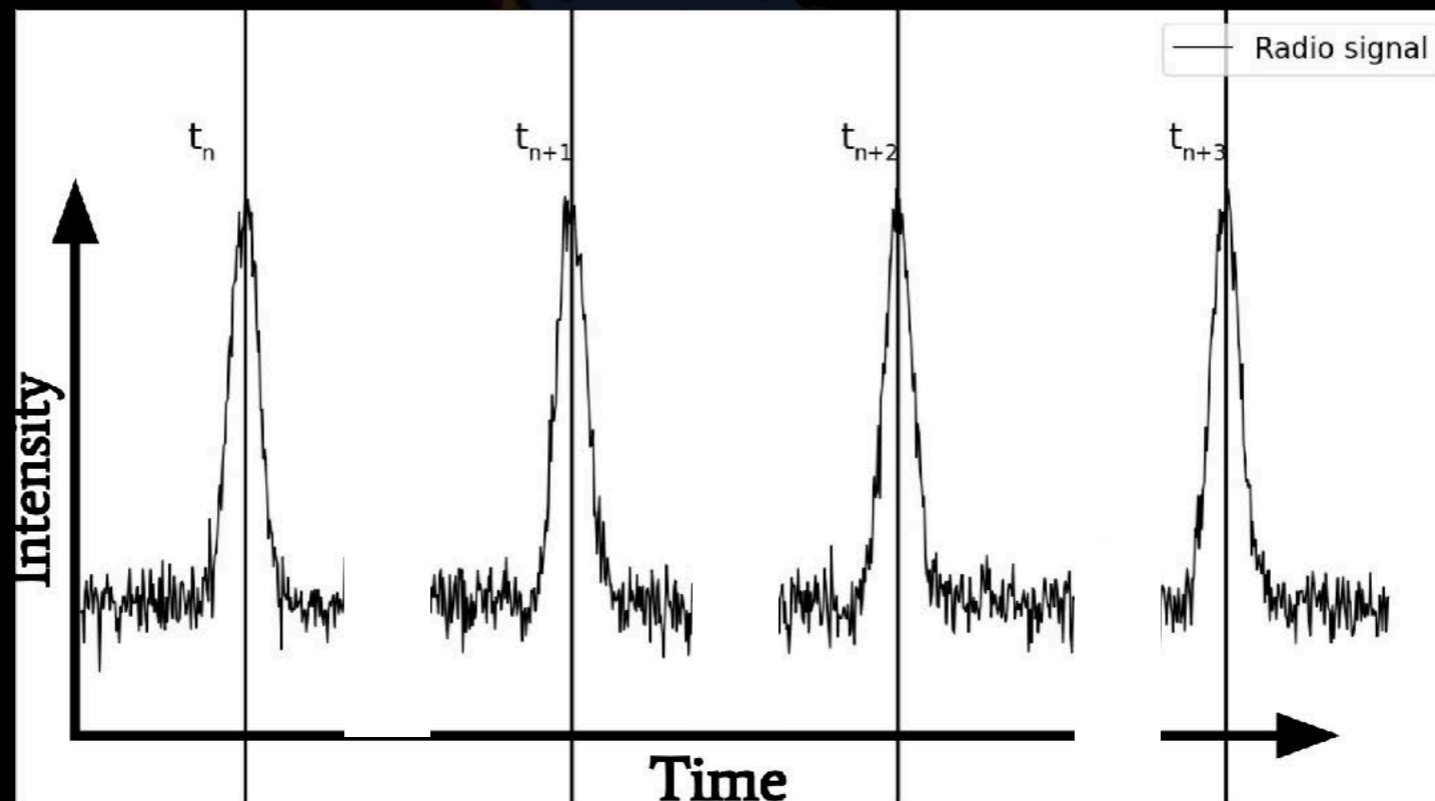
$$S_k = \frac{A^2}{12\pi^2} \frac{K_{\text{scale}}}{\nu^{-k}} \left(\frac{f}{1\text{yr}} \right)^{-\gamma} \frac{\text{yr}^3}{T_{\text{span}}} \quad \text{with } \nu \text{ the observation frequency}$$

- RN: standard red noise ($k = 0$)
- DM: Dispersion Measure variations ($k = 2$)
- SV: scattering variations ($k = 4$)

+2
+2
+2

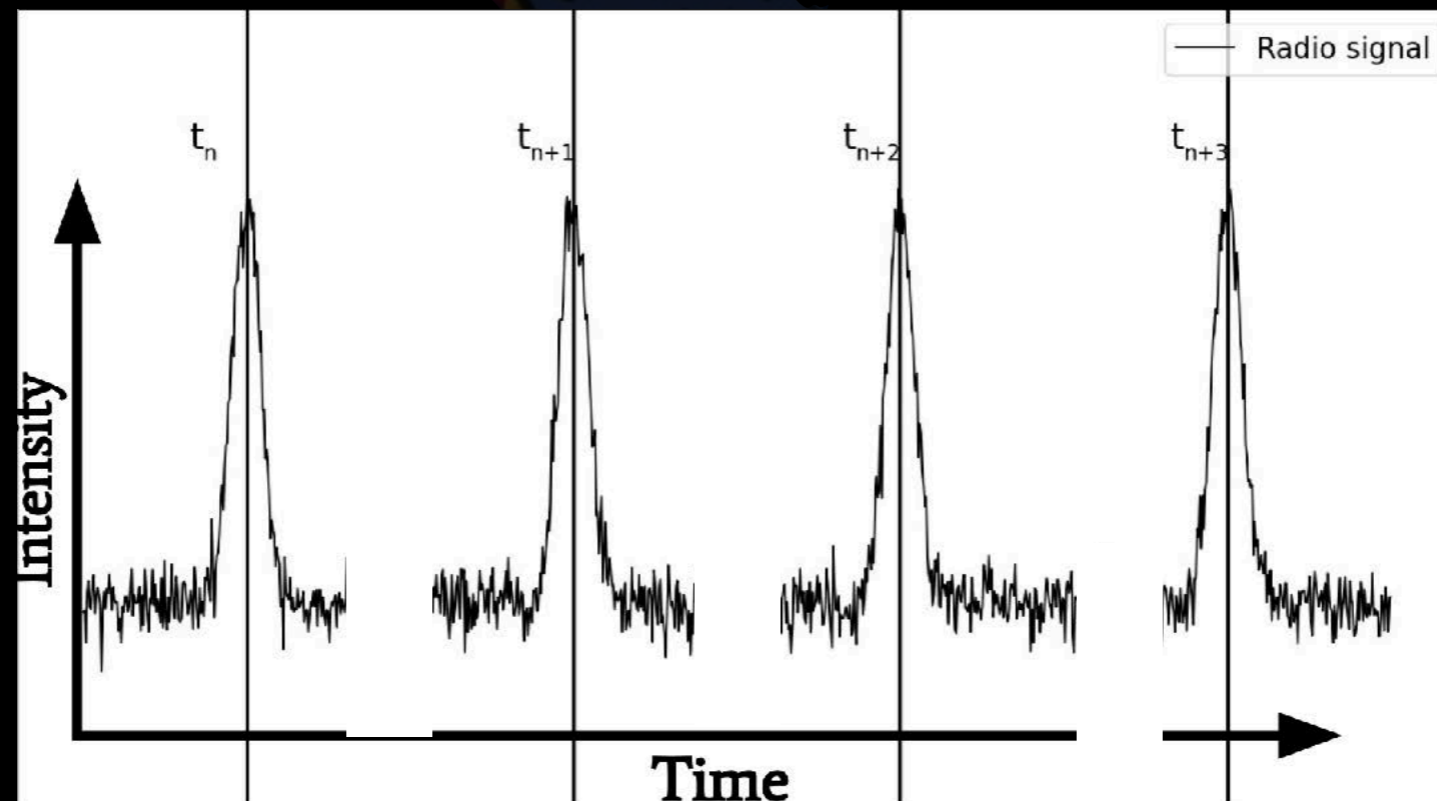
▶ Specific features for some pulsar: exponential dips

Pulsar timing and GWs



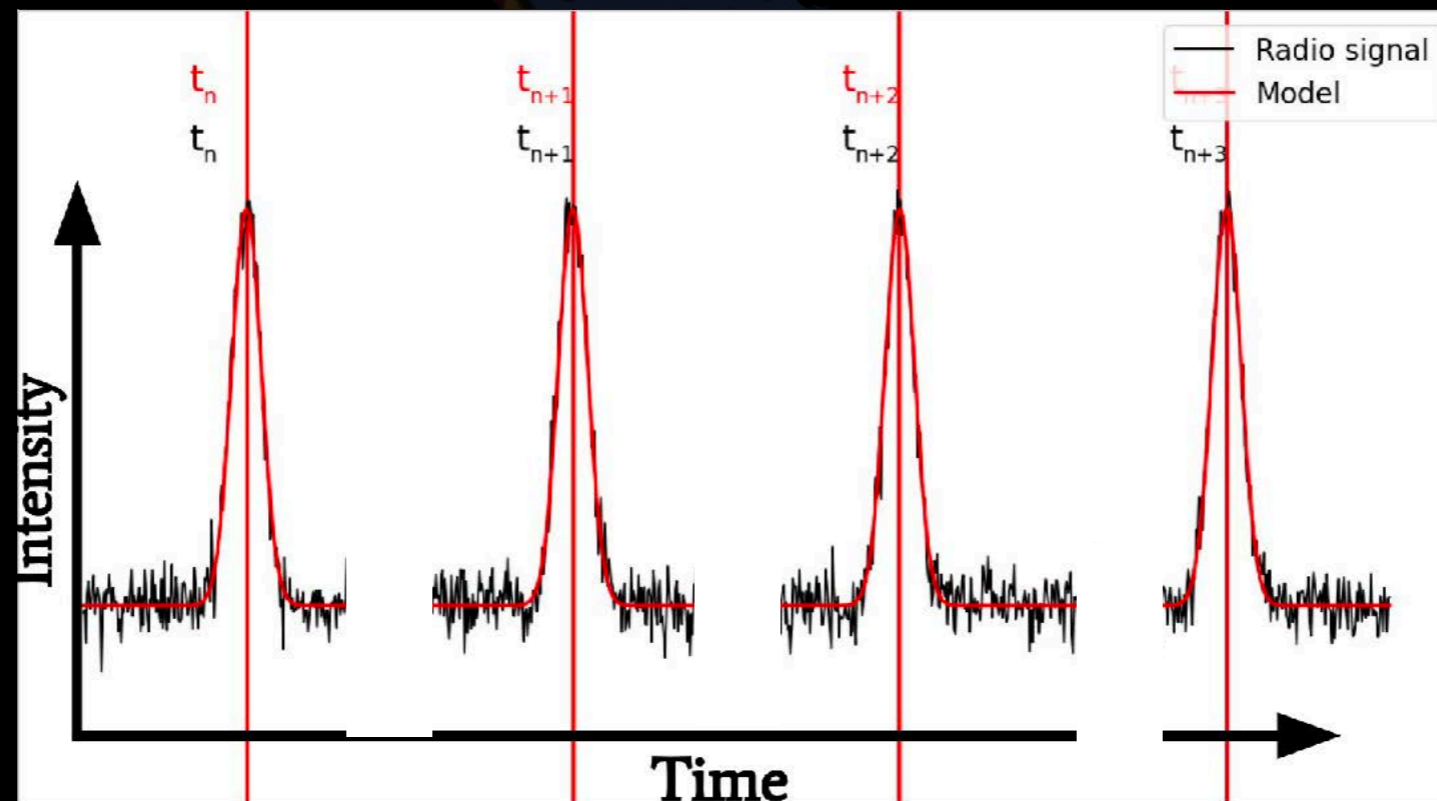
Pulsar timing and GWs

- ▶ When gravitational waves (GWs) are passing between pulsar and Earth, they will slightly **modified the arrival time of pulses**, i.e. the TOA



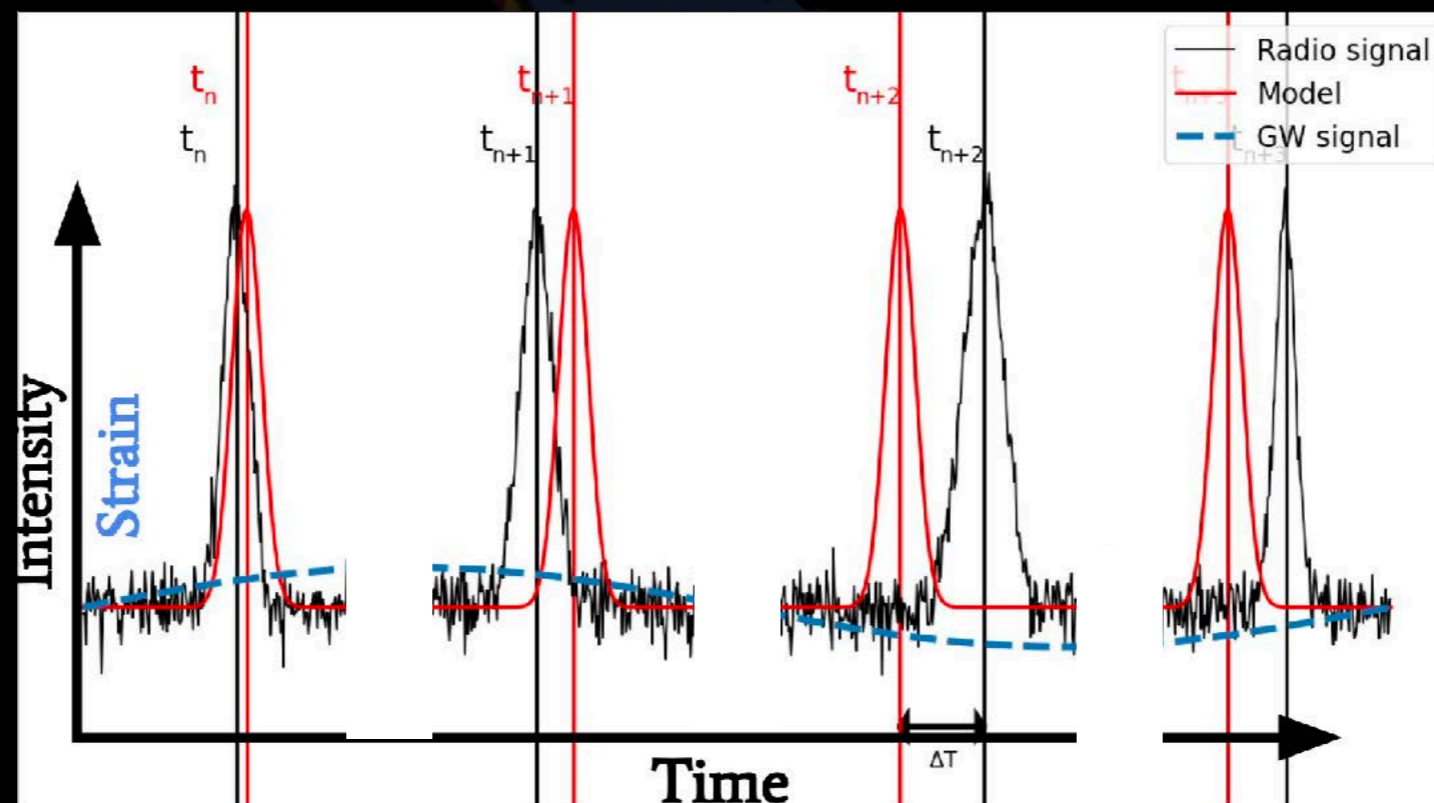
Pulsar timing and GWs

- ▶ When gravitational waves (GWs) are passing between pulsar and Earth, they will slightly **modified the arrival time of pulses**, i.e. the TOA
- ▶ We have a model for the TOA



Pulsar timing and GWs

- ▶ When gravitational waves (GWs) are passing between pulsar and Earth, they will slightly **modified the arrival time of pulses**, i.e. the TOA
- ▶ We have a model for the TOA
- ▶ If GWs => deviation from the model
=> GWs observed in the **residuals = data - model**



Pulsar timing and GWs

▶ GWs => **correlated fluctuations** in TOAs of multiple pulsars

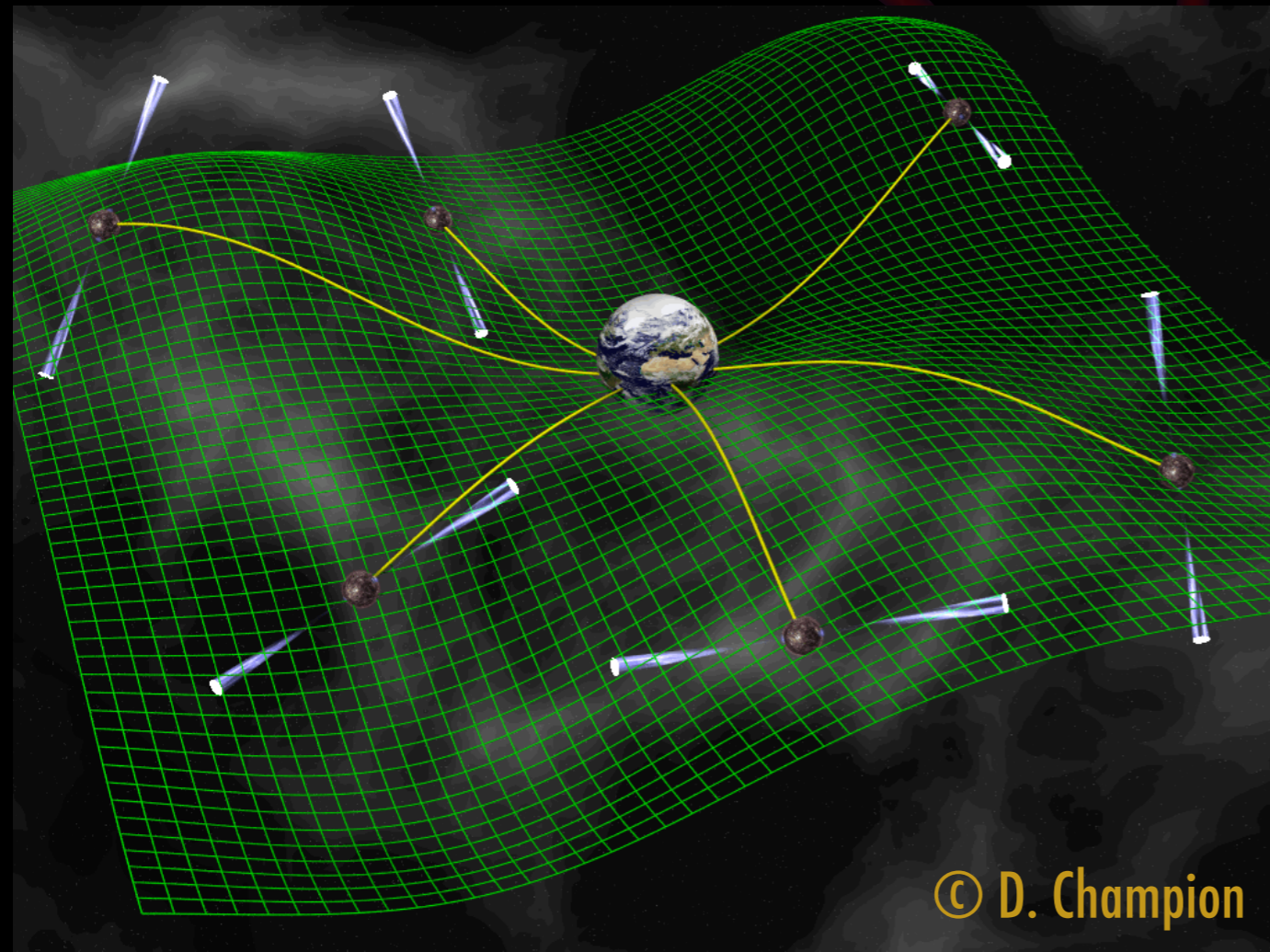
Observed & emitted pulsar spin frequency

$$\delta t_{GW}(t_a) = \int_{t_e}^{t_a} \frac{\nu(t') - \nu_0}{\nu_0} dt' = \int_{t_e}^{t_a} \frac{\delta \nu(t')}{\nu_0} dt'$$

Emission & reception times of pulses

$$\frac{\delta \nu(t')}{\nu_0} = \frac{\hat{n}_\alpha^i \hat{n}_\alpha^j}{2(1 + \hat{n}_\alpha \cdot \hat{k})} \Delta h_{ij}$$

Pulsar & GW source sky location



© D. Champion

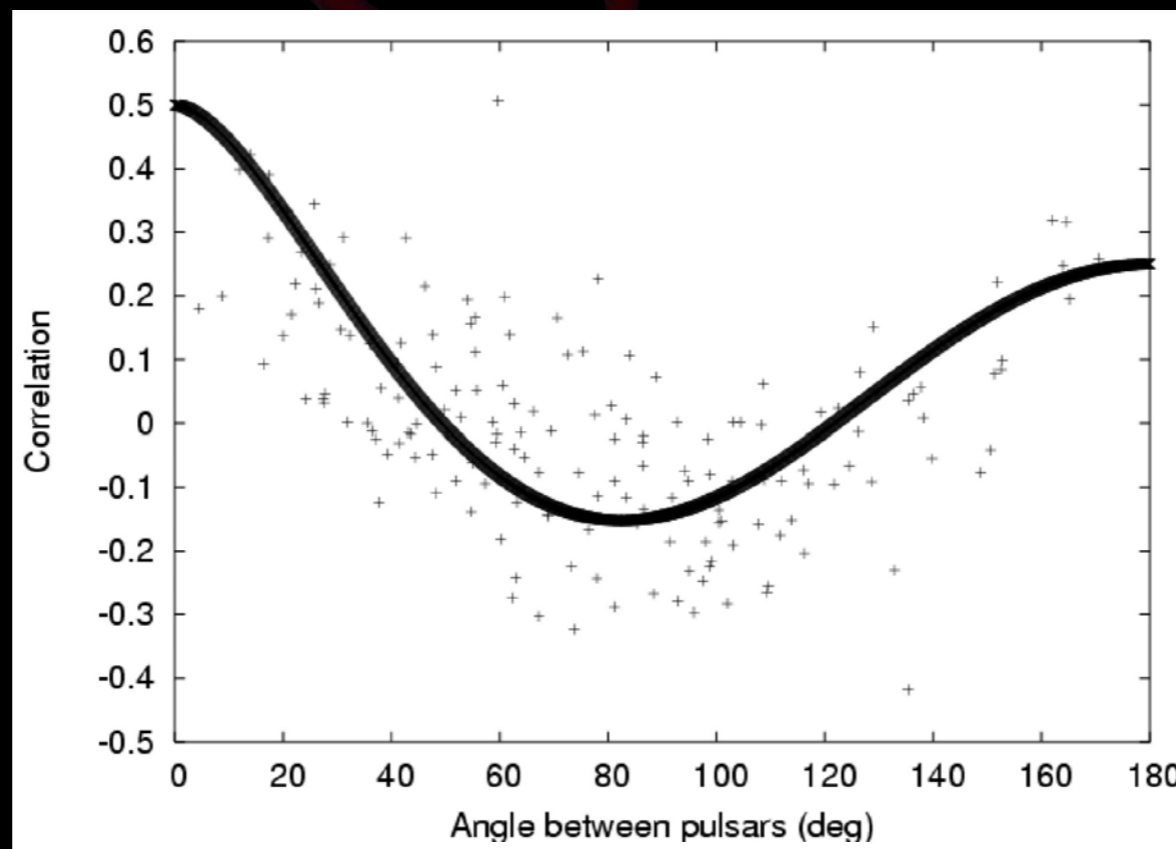
$$\Delta h_{ij} = h_{ij}(t_e) - h_{ij}(t_a)$$

GW characteristic strain

Pulsar timing and GWs

- ▶ For an **isotropic GW background**, characteristic spatial correlation: Hellings-Down curve: specific relation between correlation of 2 pulsar and their angular separation => signature of GW Background

$$\Gamma_{\text{GWB}}(\zeta_{IJ}) = \frac{3}{2}x_{IJ} \ln x_{IJ} - \frac{x_{IJ}}{4} + \frac{1}{2} + \frac{1}{2}\delta x_{IJ} \quad \text{with} \quad x_{IJ} = [1 - \cos(\zeta_{IJ})]/2$$



Correlated signals



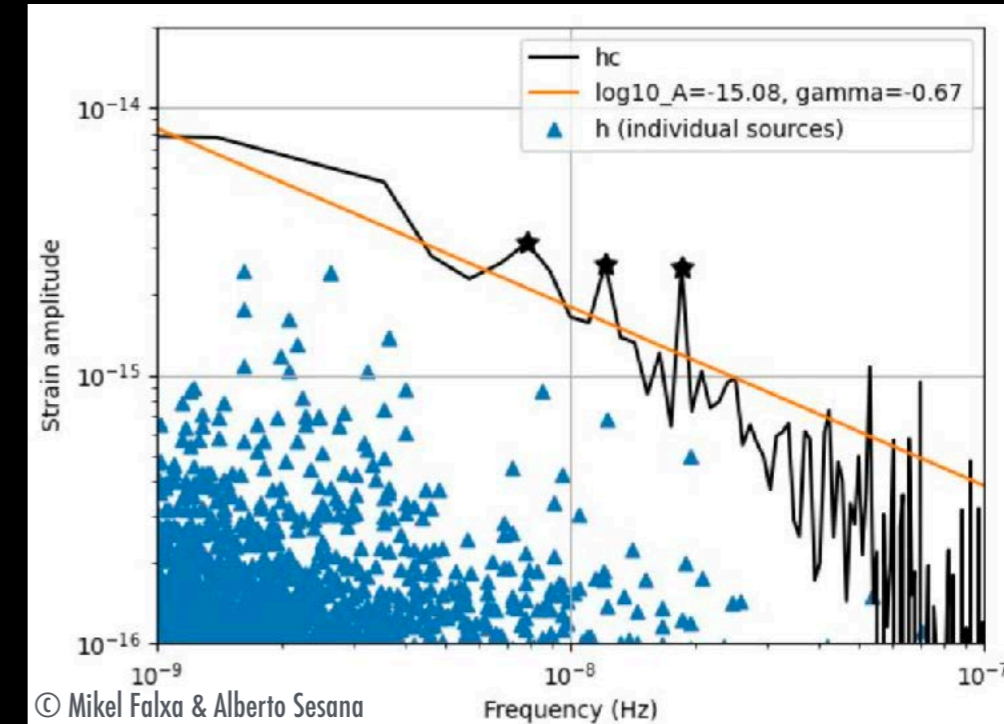
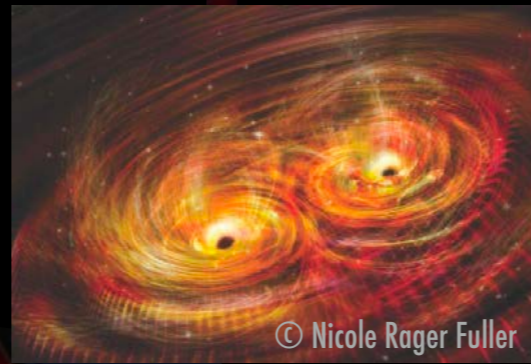
▶ 3 potential types of signal correlated between pulsars:

- **Quadrupole:**
 - Gravitational waves
- **Dipole:**
 - Systematic in the model of the position of the Earth, i.e. solar system ephemeris
- **Monopole:**
 - Clock time errors

GW sources in the nHz band

► Supermassive black hole binaries

- Ex: chirp mass = $10^9 M_{\text{Sun}}$, 1000 years before merger
- Very massive: masses $> 10^7 M_{\text{Sun}}$,
- Close: distance $z < 2$,
- Quasi-monochromatic
- Large number of sources:
 - Individual sources
 - "Stochastic" background built from large number of non-resolved sources

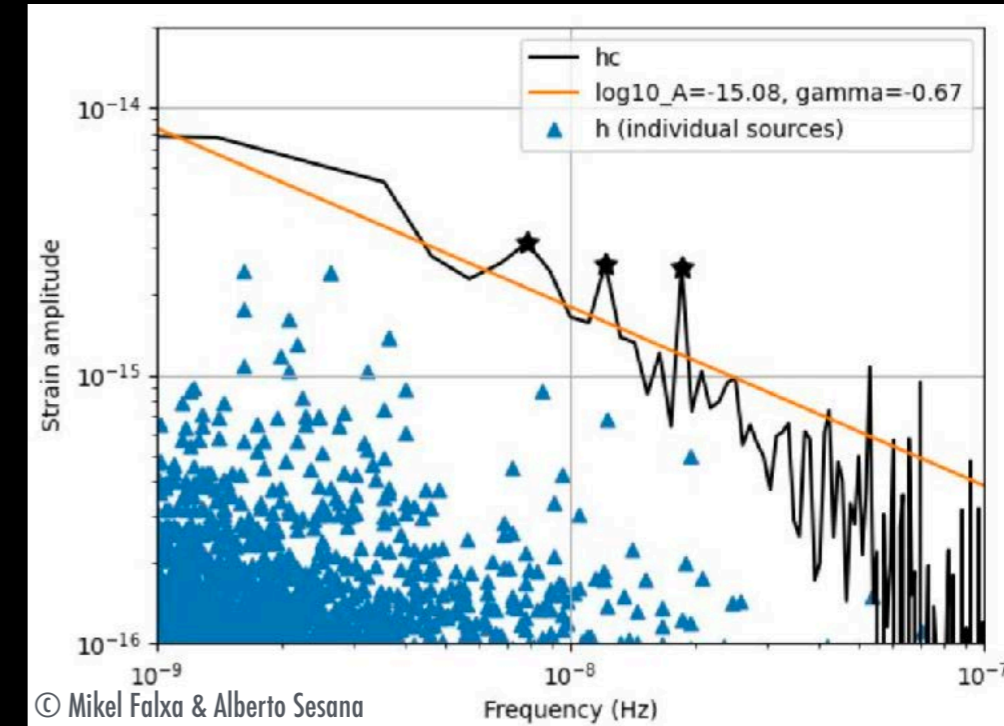


GW sources in the nHz band



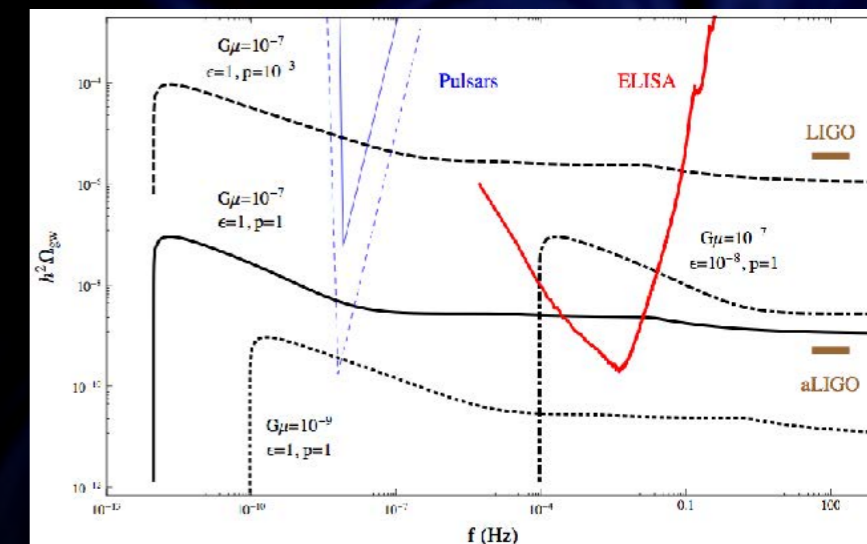
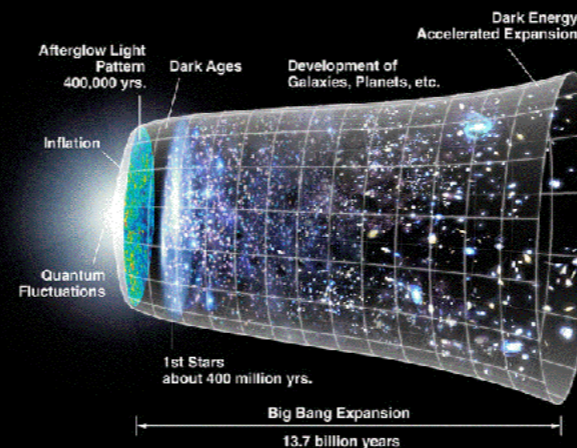
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Stochastic background from cosmological origin:

- First order phase transition
- Cosmic strings
- Primordial GWs
- ...



© Binétruy et al.

EPTA



▶ European collaboration:

- Nancay RT (FR),
70% of the data
- Effelsberg RT (G),
- Jodrell Bank Obs. (UK),
- Westerbork Synthesis
RT(NL),
- Sardinia RT (I).



IPTA



▶ Two others collaborations

- Parkes PTA (Australia)
 - Parkes radiotelescope
- NANOGrav (USA):
 - Arecibo
 - Green Bank



▶ Recent collaborations:

- InPTA: GMRT, ORT (Inde)
- CPTA: FAST, ... (Chine)
- MeerKAT (Afrique du Sud)



▶ Worldwide collaboration: International PTA

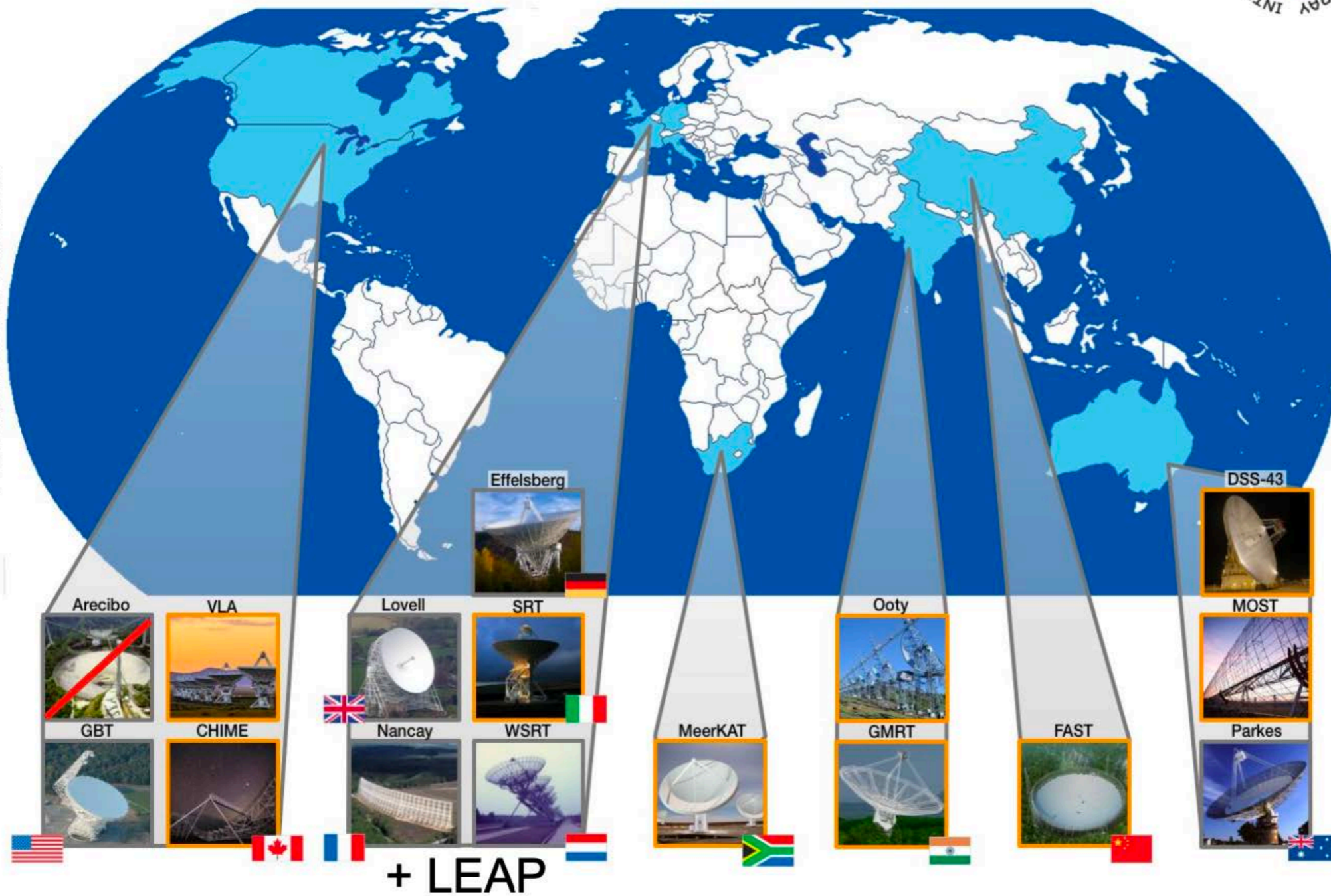
PTA collaborations



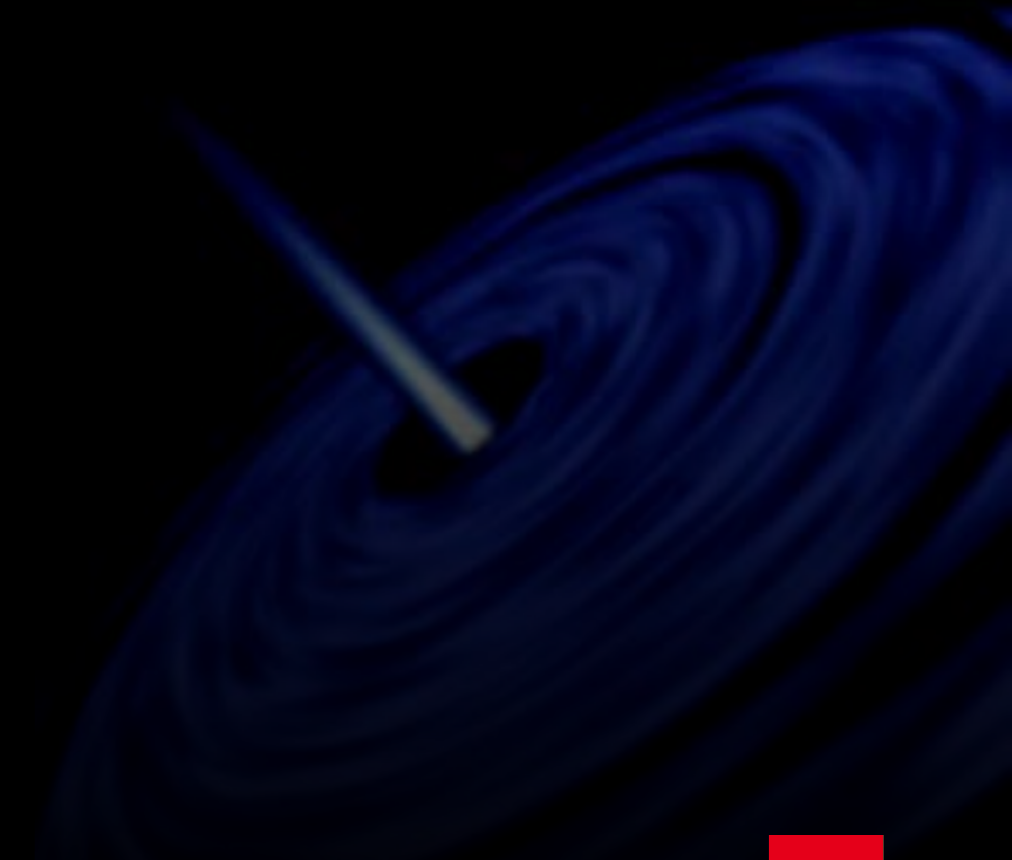
The International Pulsar Timing Array



From NANOGrav's website



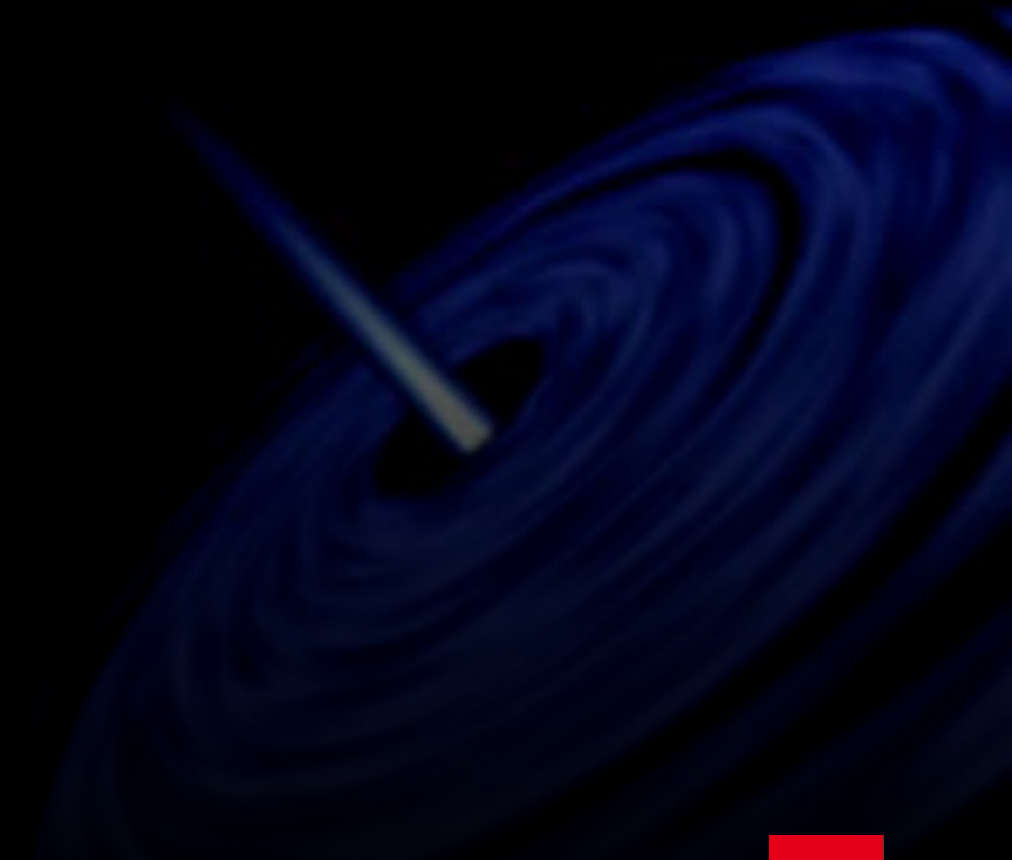
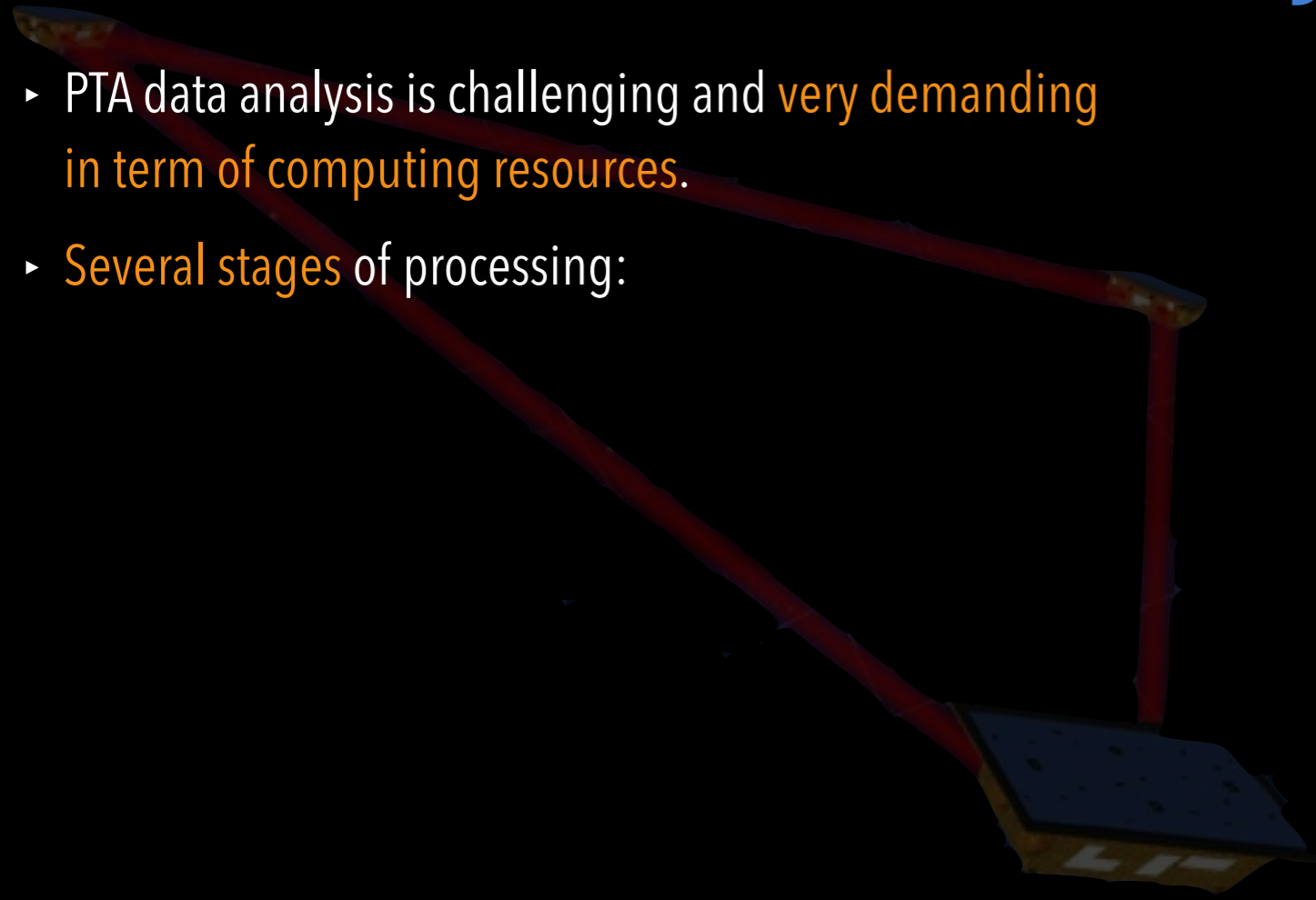
PTA data analysis



PTA data analysis



- ▶ PTA data analysis is challenging and **very demanding** in term of **computing resources**.
- ▶ **Several stages** of processing:



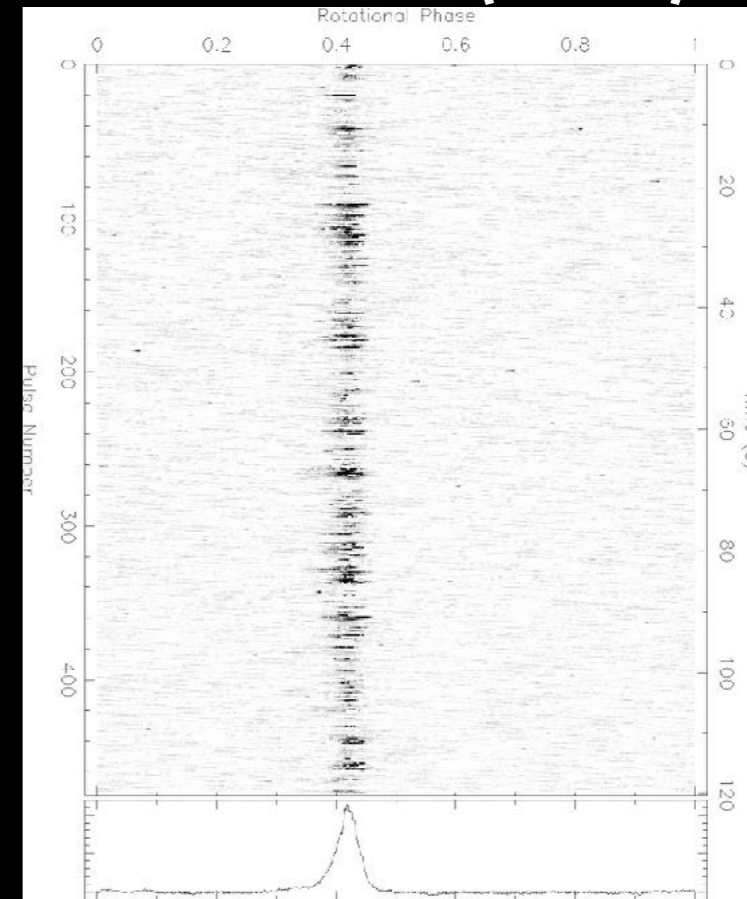
PTA data analysis



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- ▶ **Several stages** of processing:

1. **Building Time of Arrival (TOA)**: processing of the **raw data** taken during one observation to **extract the TOA** of the pulse with extremely high precision;

One observation (1.5 Go)



TOA

PTA data analysis



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TOA

PTA data analysis



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Pulsar 1



PTA data analysis

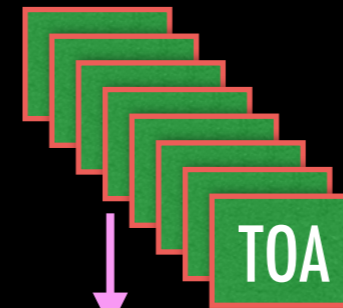


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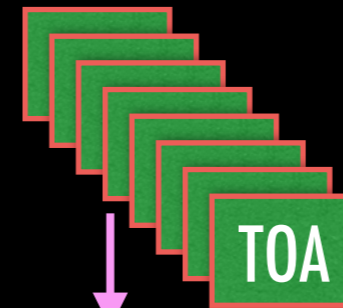
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Pulsar 1



Parameters of pulsar 1

Pulsar 2



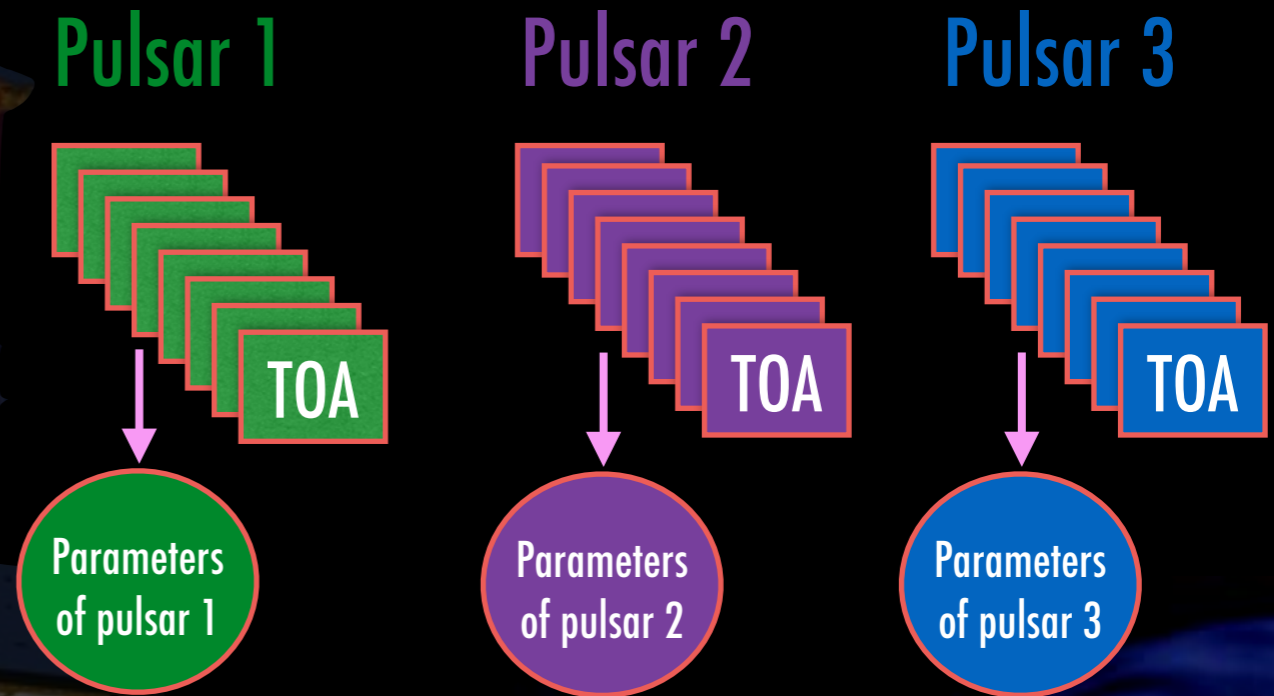
Parameters of pulsar 2

PTA data analysis

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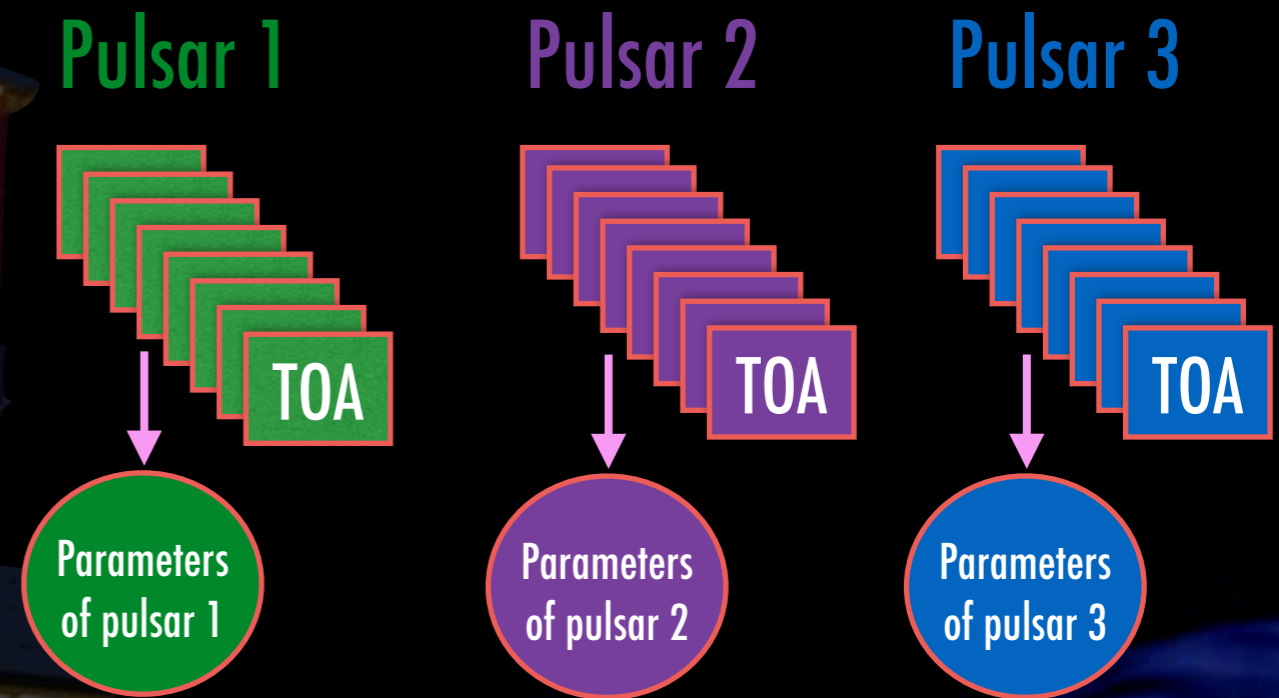


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3. **Global analysis**: processing of **all pulsars TOAs** to **estimate parameters of GW signals and global noises** (multiple types of signal; from 2 to 100 parameters) allowing some variations of some of the individual pulsar noise parameters.



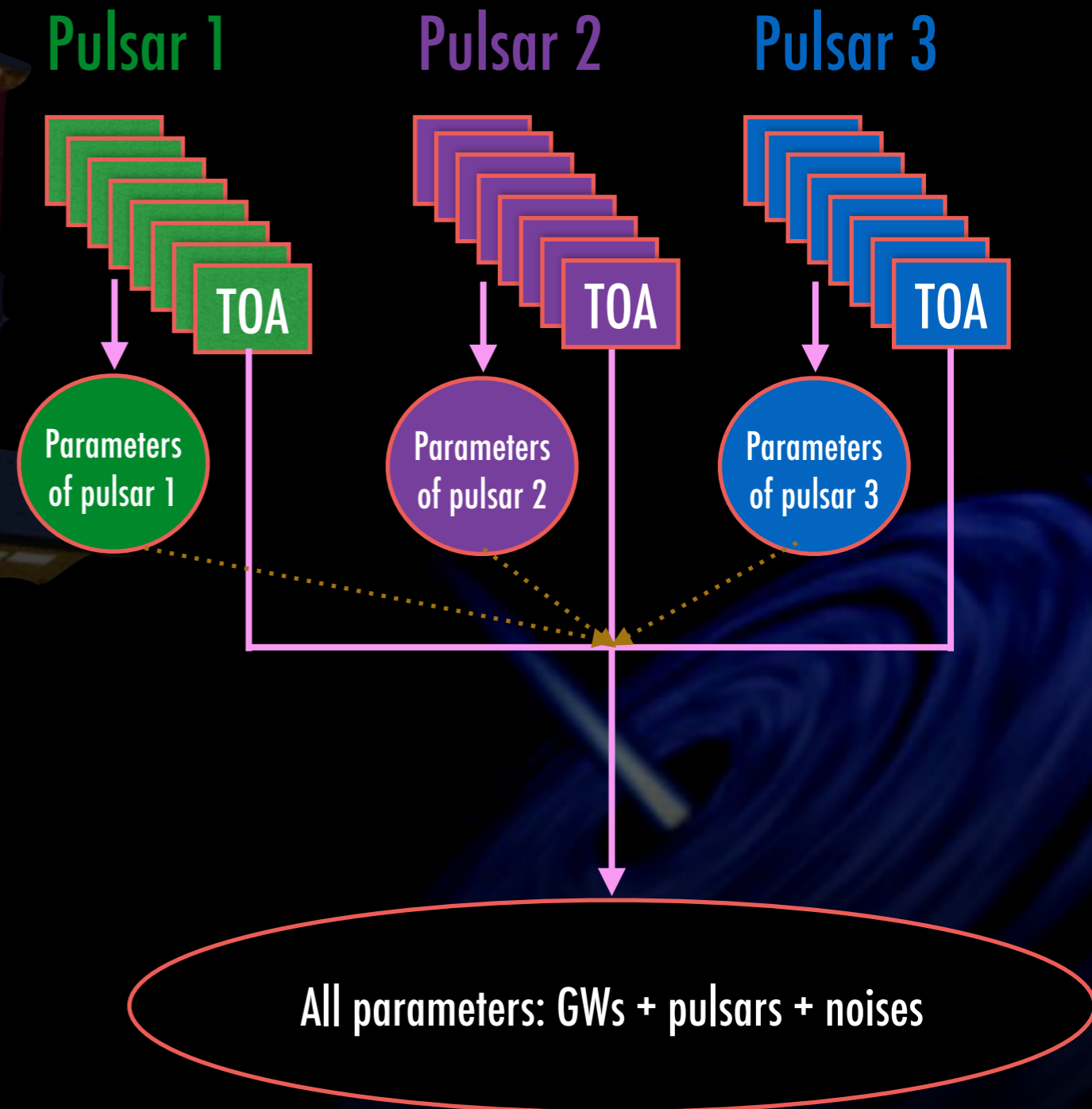
PTA data analysis

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▶ **Several tools** for each steps developed either locally or within the international collaboration



PTA data analysis



▶ (Step 3) Global analysis:

- **Systematics**: ephemerides, clock stability, ...
- **Bayesian analysis**:

$$p(\delta t | \vec{\theta}) = \frac{1}{\sqrt{\det(2\pi\Sigma)}} \exp\left(-\frac{1}{2}\delta t^T \Sigma^{-1} \delta t\right)$$

- **Continuous waves** (i.e. individual sources): $\delta t \rightarrow \delta t - \sum_{i=1}^{N_{\text{signals}}} h_i$
- **Stochastic**: Σ
 - GW Background: common noise
 - Noises:
 - White noise: measurement errors + systematics
 - Red noise: low frequency noise on pulsar rotation
 - Dispersion noise due to the propagation through interstellar medium
- **Timing parameters** (pulsars parameters) also considered

PTA data analysis



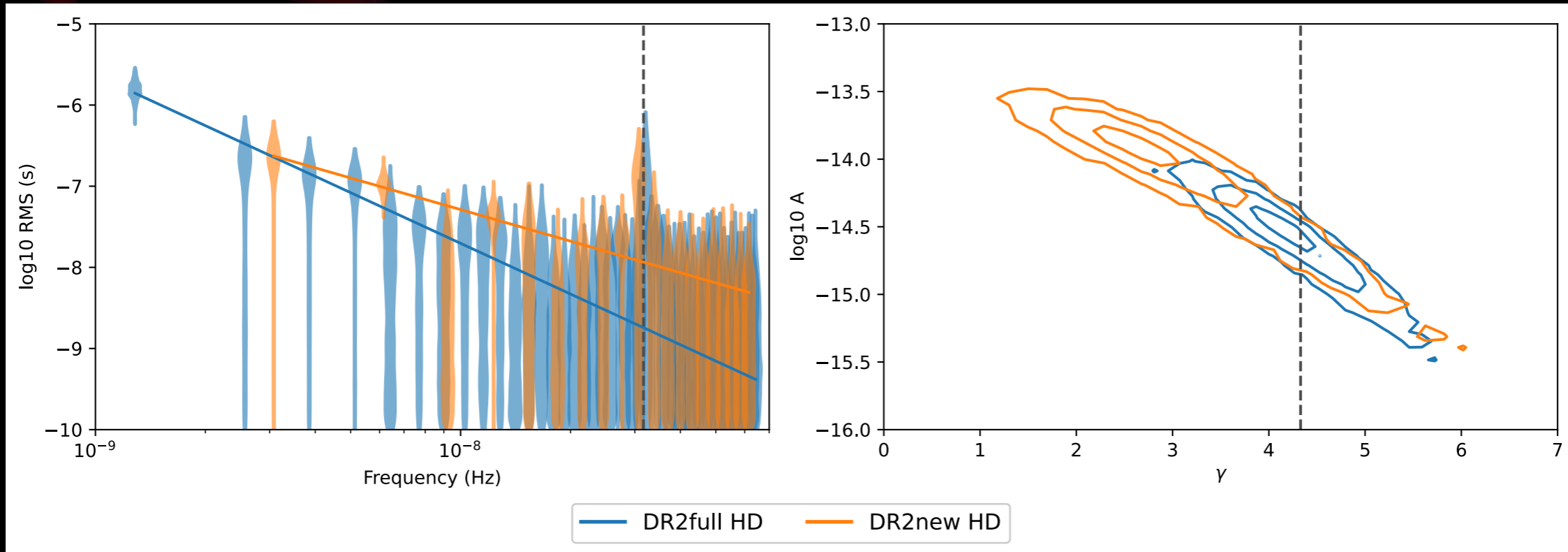
- ▶ PTA data analysis is challenging and **very demanding in term of computing resources**.
- ▶ **Several stages** of processing:
 1. Building Time of Arrival (TOA)
 2. Single pulsar analysis
 3. Global analysis
- ▶ Ideally all the processing steps to be done simultaneously BUT the trans-dimensionality and the size of the parameter space and of the model space to explore, would be enormous and **not tractable with the current methods and computing facilities**.
- ▶ Methods currently used: **Bayesian with hypermodel selection** (MCMC & nested sampling)
- ▶ Data: **30 to 60 pulsars** are currently analysed with about **5000 to 10 000 TOAs per pulsar**.
- ▶ **TOAs not regularly sampled** => likelihood computation required the inversion of a **big matrix**, Σ^{-1} ($\sim 10^5 \times 10^5$ but soon $\sim 10^6 \times 10^6$).
- ▶ Current methods are performing **some approximations** to avoid this inversion.
- ▶ Some exploration of machine learning methods, but not yet full-scale application and very low level of maturity.

EPTA results: evidence for GWs



Free spectrum

Posterior for GWB parameters

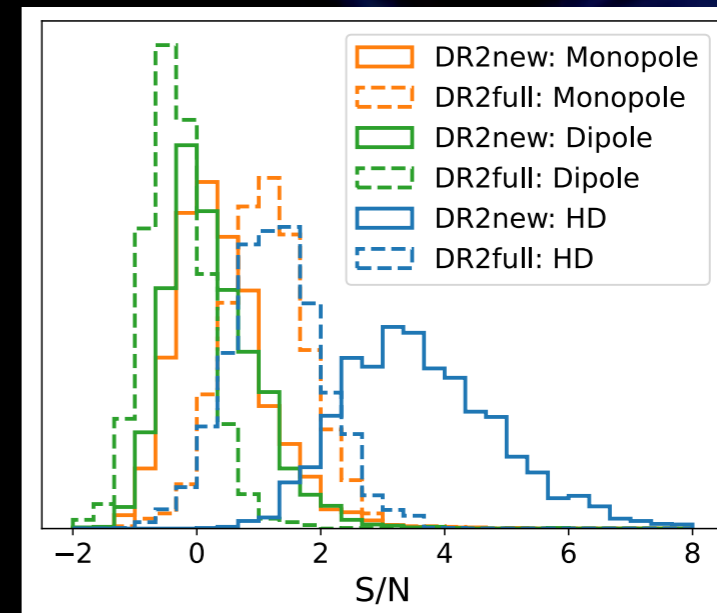


GWB parameters (DR2new):

- logarithmic amplitude: $\log_{10} A = -13.94^{+0.23}_{-0.48}$
- spectral index: $\gamma = 2.71^{+1.18}_{-0.73}$

No dipole and no monopole

<https://arxiv.org/abs/2306.16214>

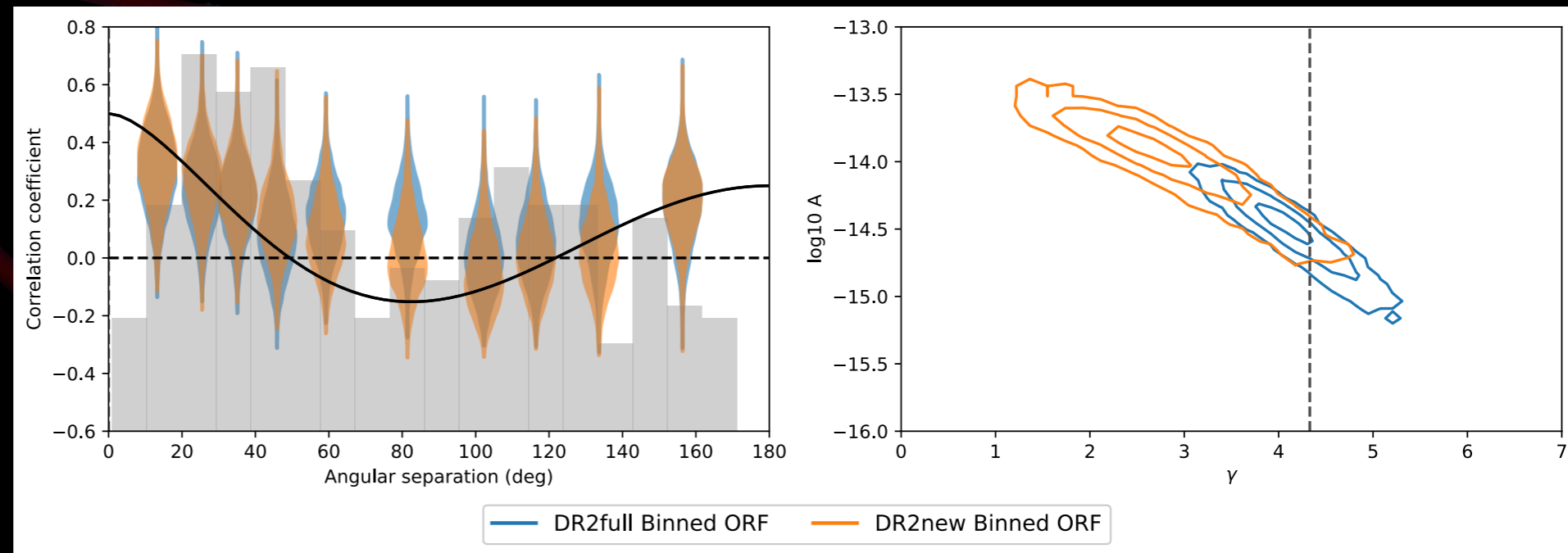


EPTA results: evidence for GWs

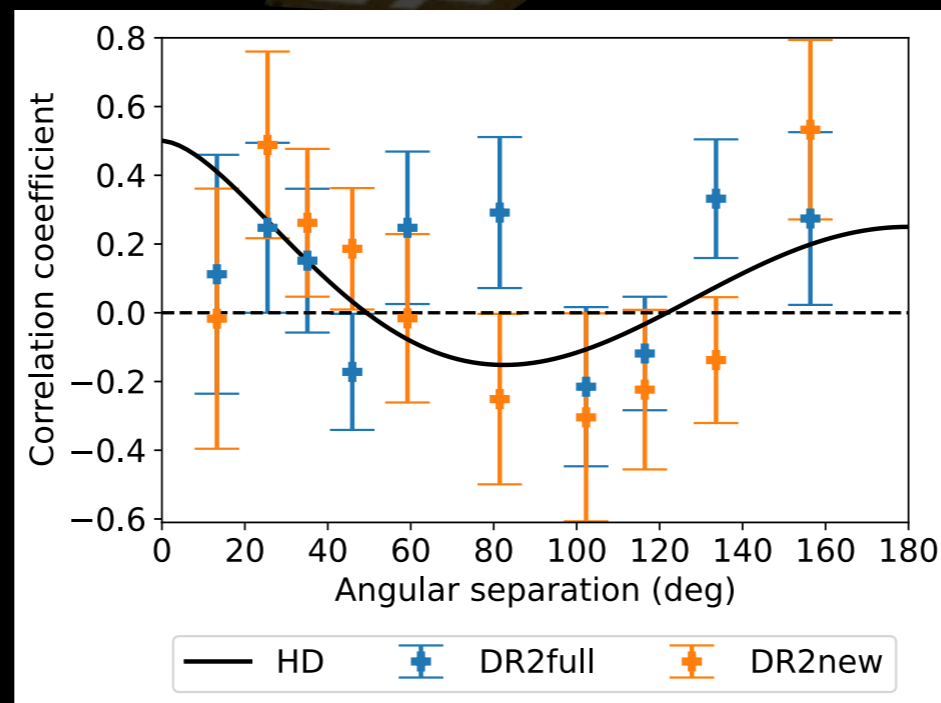


► Spatial correlation: overlap reduction function

- Binned



- Optimal statistic



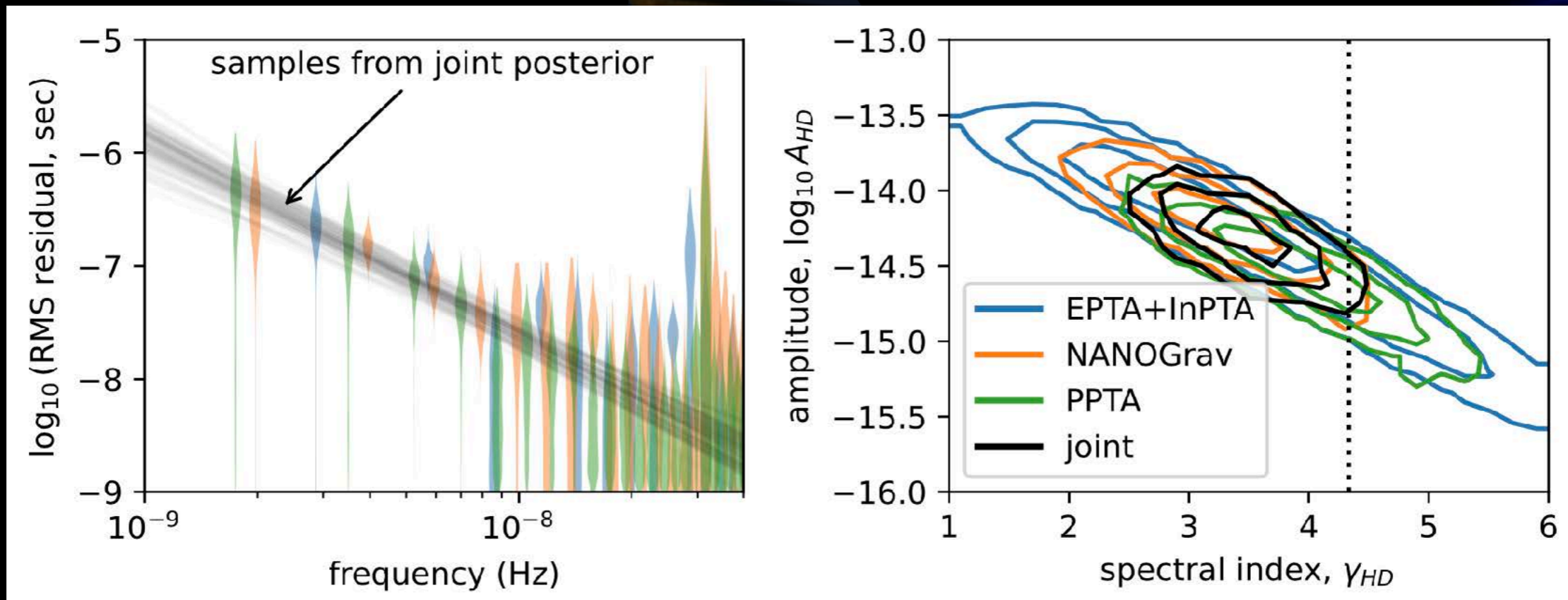
<https://arxiv.org/abs/2306.16214>

IPTA results



- ▶ **Similar results** from other PTA collaborations
- ▶ The origin of the signal is still to be understood.
- ▶ IPTA is working on a **joined analysis** :
 - All TOAs together
 - We should be able to confirm the detection and have a better characterisation soon ...
 - But complex analysis

<https://arxiv.org/abs/2309.00693>



PTA near futur



▶ More data !

- IPTA: all PTAs (EPTA, NANOGrav, PPTA) + MeerKAT + CHIME (+ FAST?)
- SKA soon (~100 pulsars with few tens thousands of TOAs per pulsar) !

▶ Also more parameters



▶ Data analysis complex and heavy: clear technical bottleneck to improve the precision and ingest all currently available data !

▶ How to address the challenge?

- More approximations? 😞
- More computing resources?
- Better data analysis strategies (ideally all steps in one!)
- ...

Conclusion and perspective



- ▶ **Similar data analysis challenges:**
 - Searching in a large parameter space
 - High precision modelling
 - Coherent integration of all steps of the analysis
- ▶ **Not the same timescale** between LISA and PTA
- ▶ LISA data analysis in a **prototyping** phase; large simulated data available
- ▶ PTA:
 - **Data already available** and more are coming in particular with SKA
 - Very close to detection => close to the scientific discovery
 - First tools available
 - Data analysis is already a challenge!



Thank you !

